

# Quantum Gravity

---

**K. Sreeman Reddy**

*E-mail:* [sreeman@brandeis.edu](mailto:sreeman@brandeis.edu)

ABSTRACT: These are some short notes on quantum gravity. I will try to review all relevant topics briefly. Perturbative string theory is the only UV finite quantum gravity theory we have (excluding toy models like SYK). Non-perturbative definitions exist for specific AdS compactifications via AdS/CFT and string field theory also gives some non-perturbative information. But non-perturbative string theory is not yet properly understood. Alternative approaches are very incomplete and inelegant compared to string theory. But I will also briefly discuss some of them. I will be continuously updating these notes when I learn new things. Which topic gets more importance will be biased based on what I am interested in. These notes are useful only to *revise* stuff that you already know, not for first-time learning. Whenever many reviews are cited, assume that the first reference is the best. For frameworks that are already empirically verified (QM, GR, and QFT), check notes at [ksr.onl/FP](http://ksr.onl/FP).

My current research area is section [8.2](#).

Please email me any mistakes you find.

Currently, these notes are in the beginning stage and are only useful to see the references cited under each section.

---

## Contents

<b>1</b>	<b>Introduction</b>	<b>2</b>
1.1	Problems	2
1.2	Expected properties	3
1.3	History	4
1.4	QFT in curved spacetime	4
1.4.1	Unruh radiation in flat space	4
1.4.2	Hawking radiation	4
1.4.3	The information paradox	4
1.4.3.1	The small corrections theorem	4
1.4.3.2	AMPS firewall	4
1.5	GR as an EFT	4
1.5.1	Universal quantum non-relativistic correction	4
1.5.2	Uncertainty in the causal structure and light cones	4
<b>I</b>	<b>String theory</b>	<b>6</b>
<b>2</b>	<b>Conformal field theory</b>	<b>6</b>
2.1	$D \geq 3$	6
2.1.1	Conformal transformations	6
2.1.2	Representations of the conformal group	7
2.1.3	Radial quantization	7
2.2	$D = 2$	7
2.2.1	Conformal transformations	7
2.2.2	Primary fields	7
2.2.3	OPE	7
2.2.4	Ward identities	7
2.2.5	Free boson	7
2.2.6	Free fermion	7
2.2.7	$2D$ superconformal field theories	7
2.2.8	The $bc$ theory	7
2.2.9	The $\beta\gamma$ theory	7
2.2.10	CFT on the Disk	7
2.2.11	CFT on the Torus	7
2.2.12	Bosonization	7
2.2.13	Entanglement entropy	7
2.3	Renormalization group	7
2.3.1	$c$ -theorem	7
2.3.2	$F$ -theorem	7
2.3.3	$a$ -theorem	7

2.3.4	Scale vs conformal invariances	7
2.4	Bootstrap	7
2.4.1	Analytic	7
2.4.2	Numerical	7
2.5	3D superconformal Chern-Simons matter theories	8
2.6	4D superconformal field theories	8
2.6.1	$\mathcal{N} = 4$ SYM	8
2.6.2	$\mathcal{N} = 2$	8
2.6.3	$\mathcal{N} = 1$	8
2.7	6D superconformal field theories	8
2.8	Axiomatic CFT	8
<b>3</b>	<b>Bosonic string theory</b>	<b>8</b>
3.1	Classical	8
3.2	Quantize	8
3.2.1	Canonical quantization	8
3.2.2	Light-cone quantization	8
3.2.3	Covariant path integral quantization	8
3.2.4	BRST quantization	8
3.3	Scattering amplitudes	8
3.3.1	Tree-level amplitudes	8
3.3.2	One-loop amplitudes	8
<b>4</b>	<b>Supersymmetry</b>	<b>8</b>
4.1	SUSY QM	8
4.2	SUSY QFT	8
4.2.1	Superspace	9
4.2.2	Gauge theories	9
4.3	SUGRA	9
4.3.1	11D	9
4.3.2	10D	9
4.3.3	4D	9
<b>5</b>	<b>Superstring theory</b>	<b>9</b>
5.1	Classical	9
5.2	Type II string theories	9
5.3	Type I string theory	9
5.4	Heterotic string theories	9
5.5	Vertex operators	9
5.6	Scattering amplitudes	9
5.6.1	Tree-level amplitudes	9
5.6.2	One-loop amplitudes	9
5.6.3	UV finiteness	9

5.7	String dualities	9
5.7.1	T-duality	9
5.7.1.1	Double field theory	9
5.7.2	S-duality	9
5.7.3	F-theory	9
<b>6</b>	<b>String landscape</b>	<b>10</b>
6.1	String compactifications	10
6.2	Nongeometric compactifications	10
6.3	String cosmology	10
6.3.1	de-Sitter vacua	10
6.3.2	String inflation	10
6.3.3	Brane cosmology	10
6.4	Particle phenomenology	10
6.4.1	Axiverse	10
6.5	Swampland	10
<b>7</b>	<b>D-branes</b>	<b>10</b>
7.1	Effective actions	10
7.2	As BPS SUGRA solitons	10
7.3	D-branes moving and merging	10
7.4	Creation/Annihilation of D-branes	10
7.5	Multiple coincident D-branes	10
7.6	D-brane geometry	10
<b>8</b>	<b>Holography</b>	<b>11</b>
8.1	Stringy AdS/CFT	11
8.1.1	Dictionary	11
8.1.2	Correlation functions	11
8.1.3	Finite temperature	11
8.1.4	Solitons	11
8.1.5	The pp wave correspondence	11
8.1.6	Different dimensions	11
8.1.6.1	$AdS_3$ compactifications	11
8.1.7	Orbifolds and orientifolds	11
8.1.8	Integrability	11
8.1.9	Higher spin duality (tensionless limit)	11
8.1.10	Fluid/gravity correspondence	11
8.1.11	Nonrelativistic limit	11
8.2	It from Qubit AdS/CFT	11
8.2.1	Holographic entanglement entropy	11
8.2.1.1	Classical gravity from entanglement	11
8.2.1.2	Quantum extremal surfaces	11

8.2.1.3	Derivation of RT, HRT, QES from gravity path integral	11
8.2.1.4	Holographic entropy cone	12
8.2.1.5	Bit threads	12
8.2.1.6	Islands	12
8.2.1.7	Quantum extremal surface perturbation theory	12
8.2.2	Tensor networks	12
8.2.3	Error correction	12
8.2.4	Chaos	12
8.2.5	Complexity	12
8.2.6	SYK	12
8.2.7	JT	12
8.2.8	DSSYK	12
8.2.9	von Neumann algebras	12
8.3	Flat space holography approaches	12
8.3.1	Celestial holography	12
8.3.2	Carrollian holography	12
8.4	de Sitter holography approaches	13
8.4.1	dS/CFT	13
8.4.2	Static patch holography	13
8.4.3	$T\bar{T}$ deformation	13
<b>9</b>	<b>Stringy maths</b>	<b>13</b>
9.1	Mirror symmetry	13
9.2	Modular forms	13
9.3	Monstrous moonshine	13
9.4	Knot theory	13
9.5	Geometric Langlands correspondence	13
9.6	K-theory	13
9.7	p-adic strings	13
9.8	Higher structures	13
9.8.1	Higher gauge theory	13
9.8.2	Higher category theory	13
9.9	Noncommutative geometry	13
9.9.1	Noncommutative algebraic geometry and mirror symmetry	14
9.9.2	Noncommutative quantum field theory	14
9.9.3	In string theory	14
<b>10</b>	<b>M-theory</b>	<b>14</b>
10.1	Membrane theory	14
10.2	Matrix theory	14
10.2.1	BFSS matrix model	14
10.2.1.1	BMN matrix model	14
10.2.2	IKKT matrix model	14

10.3	AdS/CFT approach	14
10.3.1	$AdS_4 \times S^7/\mathbb{Z}_k$ & ABJM CFT	14
10.4	Miscellaneous	14
<b>11</b>	<b>String field theory</b>	<b>14</b>
11.1	Off-shell string theory	14
11.2	Bosonic string field theory	14
11.2.1	Open	14
11.2.2	Closed	14
11.2.3	Open-Closed	14
11.2.4	Background independence	14
11.3	Superstring field theory	14
11.4	Tachyon condensation	14
<b>12</b>	<b>Miscellaneous</b>	<b>15</b>
12.1	Black holes	15
12.1.1	Microscopic origin	15
12.1.2	Wormholes in the axiverse	15
12.2	Chern-Simons theories	15
12.2.1	Quantum Gravity in 2+1 Dimensions	15
12.3	Topological string theory	15
12.3.1	Twistor string theory	15
12.3.1.1	Amplituhedron	15
12.4	More on scattering amplitudes	15
12.4.1	Double copy	15
12.5	Localization techniques	15
12.6	Generalized symmetries	16
12.7	Pure spinor formalism	16
12.8	Worldline formalism ( $\infty$ tension limit)	16
12.9	Nonrelativistic string theory	16
12.10	2D string theory	16
12.10.1	Liouville theory	16
12.10.2	CGHS gravity	16
12.11	Quantum spacetime proposals other than noncommutative geometry	16
12.11.1	Modular spacetime and metastring theory	16
12.11.2	Stringy differential geometry	16
<b>II</b>	<b>Other approaches</b>	<b>17</b>
<b>13</b>	<b>Twistor theory</b>	<b>17</b>
13.1	Real slices and reality structures	17
13.2	$\mathbb{M}_{\mathbb{C}}$ 's conformal structure = $\mathbb{PT}$ 's complex structure	17
13.3	Penrose transform	17

13.4 Gauge theory	17
13.5 Ambitwistors and $d > 4$	17
13.6 Mini-Twistor theory	17
13.7 Miscellaneous	17
<b>14 Canonical quantum gravity</b>	<b>17</b>
14.1 ADM formalism	17
14.2 Wheeler–DeWitt equation	17
<b>15 Loop quantum gravity</b>	<b>17</b>
15.1 Ashtekar variables	17
15.2 Quantum Riemannian geometry	17
15.3 Spin foams	17
15.4 Loop quantum cosmology	17
<b>16 Weinberg’s asymptotic safety</b>	<b>18</b>
<b>17 Causal set theory</b>	<b>18</b>
<b>18 Causal fermion systems</b>	<b>18</b>
<b>19 Causal dynamical triangulation</b>	<b>18</b>
<b>20 Group field theory</b>	<b>18</b>
<b>21 Unimodular gravity</b>	<b>18</b>
<b>22 Hořava–Lifshitz gravity</b>	<b>18</b>
<b>A Miscellaneous math</b>	<b>19</b>
<b>References</b>	<b>20</b>
<b>Acknowledgements</b>	<b>42</b>

---

# 1 Introduction

Nevertheless, due to the inneratomic movement of electrons, atoms would have to radiate not only electromagnetic but also gravitational energy, if only in tiny amounts. As this is hardly true in nature, it appears that **quantum theory would have to modify** not only Maxwellian electrodynamics, but also the new theory of gravitation.

---

*Albert Einstein (1916) [1]*

Gravity couples to the stress-energy tensor. So, gravity couples to everything. Except for gravity, we know that everything else in the physical world is fundamentally quantum in nature. It is probably not possible or at least inelegant to consistently couple classical gravity to quantum fields. So, we are compelled to quantize gravity.

Since it couples to everything, in principle, every calculation that we make to predict something about reality must include corrections coming from quantum gravity. For example, if you have a scalar field theory, we know how to solve the QFT if we neglect the scalar field interaction with gravity, but there will always be corrections due to the interaction between the scalar field and gravity. You can do semiclassical physics (QFT in curved spacetime), but there will still be quantum gravity corrections. But, in practice, quantum gravity effects are notoriously hard to detect in experiments. The Planck length is  $10^{16}$  times smaller than the smallest scale that our species probed. In a loose sense, any approach to quantum gravity is a theory of everything since quantum gravity is *necessary* to understand anything exactly. But usually, the term theory of everything is reserved for theories like string theory where the theory is hoped to be *sufficient* to explain all physical phenomena.

We have figured out how to quantize fields with spin  $0, \frac{1}{2}, 1$ . But quantizing the spin 2 gravitational quantum field turned out to be hard or impossible due to the perturbative nonrenormalizability of gravity. It is unlikely that there is a nontrivial UV fixed point for gravity; see section 16. So, it seems highly likely that the framework of QFT is insufficient for quantum gravity, and we have... [to go... even further beyond!](#)

I learned very early the difference between knowing the name of something and knowing something.

---

*Richard Feynman*

When I started these notes on 2024-02-20, I knew the *names* of most topics related to quantum gravity. My goal now is to properly understand them instead of just knowing the names.

## 1.1 Problems

[15–19]

Some of the many problems that we encounter when we try to quantize gravity are:

**Perturbative nonrenormalizability:**

**Unitarity of black hole evaporation:**



**Causality and chronology protection conjecture:**

**Singularities and cosmic censorship:**

**Problem of time:**

**Failure of classical spacetime:** If we try to probe a distance smaller than the Planck scale, then due to the Heisenberg uncertainty principle, the momentum and energy will be so large that this region will collapse into a black hole. So, the classical spacetime that we understand well breaks down at the Planck scale. What is the nature of quantum spacetime from which the classical spacetime emerges? Is it noncommutative geometry [9.9](#)?

**Holographic description:** Does the fact that black hole entropy scales like area really imply that quantum gravity must have a lower dimensional field theory description? Is holography limited to asymptotically AdS spacetimes (AdS/CFT)? Or is it a property of all spacetimes?

**Framework:** All approaches to quantum gravity indirectly use the framework of QFT or GR. For example, worldsheet string theory is  $2D$  CFT, and holography is  $D \geq 2$  CFT. Is there a more natural mathematical framework for quantum gravity instead of QFT?

Quantum gravity is notoriously a subject where problems vastly outnumber results.

---

*Sidney Coleman (1989)*

## 1.2 Expected properties

These are some expected properties of quantum gravity.

1. **Unitarity:**
2. **No local observables:** [\[21\]](#).
3. **UV complete:** [\[105\]](#).
4. **IR complete:** [\[22, 105, 192\]](#). Although IR divergences are normally considered to be less serious than ultraviolet ones, they certainly cannot be ignored.
5. **Holography:** [\[23–25\]](#). Historically, holography was first argued [\[26\]](#) based on black hole thermodynamics without invoking string theory.
6. **No global symmetries:** Check [6.5](#).
7. **Completeness of spectrum:** Check [6.5](#).
8. **Weak gravity conjecture:** Check [6.5](#).
9. **Moduli space is non-compact and simply connected:** Check [6.5](#).
10. **Infinite tower of states (Distance conjecture):** Check [6.5](#).
11. **Finiteness and string lamppost:** Check [6.5](#).

12. **Uncertainty in the causal structure and light cones:** Check [1.5.2](#).
13. **No quantum metric:** [\[56\]](#).
14. **No test mass limit:** [\[56\]](#).

### **1.3 History**

[\[27–36\]](#)

I do not want to discuss history. But check the above references. There are many interesting historical facts like how string theory was originally developed to explain the strong force instead of quantum gravity.

### **1.4 QFT in curved spacetime**

[\[37–55\]](#)

Even though Hawking radiation has not yet been experimentally observed, almost every reasonable physicist believes in its validity. So, this section could be, in principle, moved to my [FP](#) notes. But it is highly relevant to quantum gravity.

#### **1.4.1 Unruh radiation in flat space**

#### **1.4.2 Hawking radiation**

#### **1.4.3 The information paradox**

##### **1.4.3.1 The small corrections theorem**

[\[44–46\]](#)

##### **1.4.3.2 AMPS firewall**

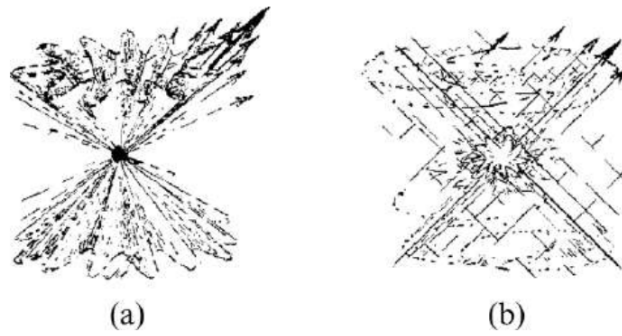
### **1.5 GR as an EFT**

[\[56–59\]](#)

#### **1.5.1 Universal quantum non-relativistic correction**

#### **1.5.2 Uncertainty in the causal structure and light cones**

[\[60\]](#)



**Fig. 33.7** (a) It has been a common viewpoint, with regard to the possible nature of a ‘quantized spacetime’, that it should be some kind of a spacetime with a ‘fuzzy’ metric, leading to some sort of ‘fuzzy’ light cone, where the notion of a direction at a point being null, timelike, or spacelike would be subject to quantum uncertainties. (b) A more ‘twistorial’ perspective would be to take the twistor space (in this case  $\mathbb{P}\mathbb{N}$ ) to retain some kind of existence (so there would still be light rays), but the condition of their intersection would become subject to quantum uncertainties. Accordingly the notion of ‘spacetime point’ would instead become ‘fuzzy’.

Figure 1. From [367]

## Part I

# String theory

References: [2, 3] are the standard references. [4, 5] are also very good and cover later understanding of non-perturbative and holographic stuff. Also see [6–14][205]

Why string theory? I will briefly mention some promising reasons. Check [61–63] for more.

- 1.

## 2 Conformal field theory

[64–71, 84]

The worldsheet descriptions of bosonic/superstring theories are 2D CFTs.  $D > 2$  CFTs are the holographic duals of superstring theories with more than 3 noncompact dimensions. So, both cases are important. I will also discuss supersymmetric CFT in this section; maybe section 4 should be before this section.

### 2.1 $D \geq 3$

#### 2.1.1 Conformal transformations

**Definition:** A conformal transformation is a specific combination of a **general coordinate** and a **Weyl transformation** that leaves the metric intact. Usually, this metric is the flat Minkowski metric.<sup>1</sup>

Almost everywhere, people specify that conformal transformation is a type of coordinate transformation. **But obviously it is not.** Every physical theory (not just general relativity) has diffeomorphism invariance, and you can check the beginning of the General relativity chapter in my [FP notes](#) if you want to know why every physical theory from Newtonian mechanics has diffeomorphism invariance. If conformal transformation is just a subset of coordinate transformation, then conformal symmetry will be present in every theory, and that is nonsense. A **mere coordinate transformation** can never change distances, as  $ds^2$  is invariant under coordinate transformations. So, you can never scale distances with them. But a **Weyl transformation changes the distances** because it directly changes the metric without changing the coordinates. Weyl symmetry **implies** conformal symmetry, but the converse is not true.

If we take the subset of conformal transformations where the Weyl part of the transformation is **trivial**, then you get a subset of diffeomorphisms that locally scale the metric. But every CFT has the full diffeomorphism invariance, not just this subset.

---

<sup>1</sup>The first time I saw this definition was in [144] in my undergrad final year, and it resolved my long-standing confusion about this definition.

**2.1.2 Representations of the conformal group**

**2.1.3 Radial quantization**

**2.2  $D = 2$**

**2.2.1 Conformal transformations**

**2.2.2 Primary fields**

**2.2.3 OPE**

**2.2.4 Ward identities**

**2.2.5 Free boson**

**2.2.6 Free fermion**

**2.2.7  $2D$  superconformal field theories**

**2.2.8 The  $bc$  theory**

**2.2.9 The  $\beta\gamma$  theory**

**2.2.10 CFT on the Disk**

**2.2.11 CFT on the Torus**

**2.2.12 Bosonization**

**2.2.13 Entanglement entropy**

**2.3 Renormalization group**

**2.3.1  $c$ -theorem**

[72, 73][165]

**2.3.2  $F$ -theorem**

[74]

**2.3.3  $a$ -theorem**

[72, 73][165]

**2.3.4 Scale vs conformal invariances**

[72]

**2.4 Bootstrap**

**2.4.1 Analytic**

[75, 76]

**2.4.2 Numerical**

[77, 78]

## 2.5 3D superconformal Chern-Simons matter theories

[79] and section 12.2.

## 2.6 4D superconformal field theories

### 2.6.1 $\mathcal{N} = 4$ SYM

[80]

### 2.6.2 $\mathcal{N} = 2$

[81]

### 2.6.3 $\mathcal{N} = 1$

[82]

## 2.7 6D superconformal field theories

[83]

## 2.8 Axiomatic CFT

[84–86][67]

## 3 Bosonic string theory

### 3.1 Classical

### 3.2 Quantize

For this part [9] is the best.

#### 3.2.1 Canonical quantization

#### 3.2.2 Light-cone quantization

#### 3.2.3 Covariant path integral quantization

#### 3.2.4 BRST quantization

### 3.3 Scattering amplitudes

#### 3.3.1 Tree-level amplitudes

#### 3.3.2 One-loop amplitudes

## 4 Supersymmetry

### 4.1 SUSY QM

[87, 88, 91, 205]

### 4.2 SUSY QFT

[89–94]

### 4.2.1 Superspace

[95]

### 4.2.2 Gauge theories

## 4.3 SUGRA

[96–102]

### 4.3.1 11D

[99, 100]

### 4.3.2 10D

### 4.3.3 4D

## 5 Superstring theory

There are no open strings in IIA, IIB in perturbation theory around the vacuum. Type II does include open strings. However, they don't show up in the vacuum perturbation theory, they are only there in connection with non-perturbative effects like D-branes.

### 5.1 Classical

[7]

### 5.2 Type II string theories

### 5.3 Type I string theory

### 5.4 Heterotic string theories

### 5.5 Vertex operators

### 5.6 Scattering amplitudes

#### 5.6.1 Tree-level amplitudes

#### 5.6.2 One-loop amplitudes

#### 5.6.3 UV finiteness

[105, 106]

### 5.7 String dualities

#### 5.7.1 T-duality

##### 5.7.1.1 Double field theory

[107–109]

#### 5.7.2 S-duality

#### 5.7.3 F-theory

[110]

## 6 String landscape

### 6.1 String compactifications

[111–117]

#### Freund–Rubin compactification

### 6.2 Nongeometric compactifications

[118–120]

### 6.3 String cosmology

[121–130]

#### 6.3.1 de-Sitter vacua

[122, 123]

#### 6.3.2 String inflation

[124, 125]

#### 6.3.3 Brane cosmology

### 6.4 Particle phenomenology

[131–133]

The previous section was on the phenomenology of cosmology. Unlike other quantum gravity theories, string theory, being a ToE, must also answer questions of particle phenomenology.

#### 6.4.1 Axiverse

[134, 135]

### 6.5 Swampland

[136–140]

## 7 *D*-branes

[5, 141, 142]

### 7.1 Effective actions

### 7.2 As BPS SUGRA solitons

### 7.3 *D*-branes moving and merging

### 7.4 Creation/Annihilation of *D*-branes

### 7.5 Multiple coincident *D*-branes

### 7.6 *D*-brane geometry

[267]



## 8 Holography

### 8.1 Stringy AdS/CFT

[5, 143–150]

#### 8.1.1 Dictionary

#### 8.1.2 Correlation functions

#### 8.1.3 Finite temperature

#### 8.1.4 Solitons

[151]

#### 8.1.5 The pp wave correspondence

#### 8.1.6 Different dimensions

##### 8.1.6.1 $AdS_3$ compactifications

[152, 153]

#### 8.1.7 Orbifolds and orientifolds

#### 8.1.8 Integrability

[154]

#### 8.1.9 Higher spin duality (tensionless limit)

[155–159]

#### 8.1.10 Fluid/gravity correspondence

[160]

#### 8.1.11 Nonrelativistic limit

[350, 351] and section 12.9

### 8.2 It from Qubit AdS/CFT

[161]

#### 8.2.1 Holographic entanglement entropy

[161–166]

##### 8.2.1.1 Classical gravity from entanglement

##### 8.2.1.2 Quantum extremal surfaces

##### 8.2.1.3 Derivation of RT, HRT, QES from gravity path integral

[161, 164]. Original articles are [167–169]

#### **8.2.1.4 Holographic entropy cone**

#### **8.2.1.5 Bit threads**

#### **8.2.1.6 Islands**

[161, 164]. Criticism about massive islands etc is discussed in [54, 170–173]

#### **8.2.1.7 Quantum extremal surface perturbation theory**

[174]

### **8.2.2 Tensor networks**

[161, 175, 176]

### **8.2.3 Error correction**

[175–177]

### **8.2.4 Chaos**

[178–180]

### **8.2.5 Complexity**

[161, 181, 182]

### **8.2.6 SYK**

[184, 185]

### **8.2.7 JT**

[183–185]. Check section 12.10.

### **8.2.8 DSSYK**

[186]

### **8.2.9 von Neumann algebras**

[187–189] these are holography related. For math [190]

## **8.3 Flat space holography approaches**

### **8.3.1 Celestial holography**

[191–196]

### **8.3.2 Carrollian holography**

[197–199]

## 8.4 de Sitter holography approaches

[200, 201]

### 8.4.1 dS/CFT

### 8.4.2 Static patch holography

### 8.4.3 $T\bar{T}$ deformation

[202]

## 9 Stringy maths

[203, 204]

### 9.1 Mirror symmetry

[205–217]

### 9.2 Modular forms

[218][214]

### 9.3 Monstrous moonshine

[219–222]

### 9.4 Knot theory

[223, 224] and section 12.2.

### 9.5 Geometric Langlands correspondence

[225–228]

### 9.6 K-theory

[229, 230]

### 9.7 p-adic strings

[231–234]

### 9.8 Higher structures

[235–242, 337]

#### 9.8.1 Higher gauge theory

#### 9.8.2 Higher category theory

### 9.9 Noncommutative geometry

[243–245]

### 9.9.1 Noncommutative algebraic geometry and mirror symmetry

[246][212]

### 9.9.2 Noncommutative quantum field theory

[247–267, 281–283]

### 9.9.3 In string theory

## 10 M-theory

### 10.1 Membrane theory

[268–278]<sup>2</sup>

### 10.2 Matrix theory

[279–285] [256, 257]

#### 10.2.1 BFSS matrix model

##### 10.2.1.1 BMN matrix model

#### 10.2.2 IKKT matrix model

### 10.3 AdS/CFT approach

[286–290]

#### 10.3.1 $AdS_4 \times S^7/\mathbb{Z}_k$ & ABJM CFT

### 10.4 Miscellaneous

[291–294]

## 11 String field theory

[14, 295–304]

### 11.1 Off-shell string theory

### 11.2 Bosonic string field theory

#### 11.2.1 Open

#### 11.2.2 Closed

#### 11.2.3 Open-Closed

#### 11.2.4 Background independence

### 11.3 Superstring field theory

### 11.4 Tachyon condensation

[305–309]

---

<sup>2</sup>Fun fact: [268] was posted on arXiv on the same day I was born (23rd Jan 2002) just few hours after I was born.

Doubt: Is there a holographic dual of bosonic string theory? The bosonic string is unstable non-perturbatively. So, it might not have a holographic dual. Sen's conjecture and instability of the D25-branes. But maybe there is still some unstable CFT with tachyons that is its dual? The R symmetry of the boundary theory will match to the symmetry of the compact dimensions. Since here we don't have R symmetry does that mean the bulk has no compactification? Does that mean the boundary theory is a 25-dimensional unstable CFT?

## **12 Miscellaneous**

### **12.1 Black holes**

[310–312]

#### **12.1.1 Microscopic origin**

#### **12.1.2 Wormholes in the axiverse**

[313, 314]

### **12.2 Chern-Simons theories**

[315–318] and also sections 2.5 and 9.4.

#### **12.2.1 Quantum Gravity in 2+1 Dimensions**

[319–323]

### **12.3 Topological string theory**

[324–326]

#### **12.3.1 Twistor string theory**

[366]

##### **12.3.1.1 Amplituhedron**

[327, 328]

### **12.4 More on scattering amplitudes**

[329–332]

#### **12.4.1 Double copy**

[333]

### **12.5 Localization techniques**

[334]

#### **12.5.1 Gromov-Witten invariants**

[335]

## 12.5.2 Localization and AdS/CFT

[336]

## 12.6 Generalized symmetries

[337–342]

## 12.7 Pure spinor formalism

[343–345]

## 12.8 Worldline formalism ( $\infty$ tension limit)

[346–349]

## 12.9 Nonrelativistic string theory

[350, 351]

## 12.10 $2D$ string theory

[352, 353]. JT gravity is in section 8.2.7.

### 12.10.1 Liouville theory

[354–356]

### 12.10.2 CGHS gravity

[357, 358]

## 12.11 Quantum spacetime proposals other than noncommutative geometry

Section 9.9 covers noncommutative geometry. Here, we will discuss alternative quantum spacetime proposals inspired by string theory.

### 12.11.1 Modular spacetime and metastring theory

[359]

### 12.11.2 Stringy differential geometry

[360]

## Part II

# Other approaches

### 13 Twistor theory

[361–368][7, 250]

#### 13.1 Real slices and reality structures

#### 13.2 $\mathbb{M}_{\mathbb{C}}$ 's conformal structure = $\mathbb{P}\mathbb{T}$ 's complex structure

#### 13.3 Penrose transform

#### 13.4 Gauge theory

#### 13.5 Ambitwistors and $d > 4$

[369]

#### 13.6 Mini-Twistor theory

[370–374]

#### 13.7 Miscellaneous

[375–377]

### 14 Canonical quantum gravity

[378, 379]

#### 14.1 ADM formalism

[380]

#### 14.2 Wheeler–DeWitt equation

### 15 Loop quantum gravity

[381–389]

#### 15.1 Ashtekar variables

#### 15.2 Quantum Riemannian geometry

#### 15.3 Spin foams

#### 15.4 Loop quantum cosmology

[390]

## 16 Weinberg's asymptotic safety

[391–393]

Also called nonperturbative renormalizability.

## 17 Causal set theory

[394, 395]

## 18 Causal fermion systems

[396, 397]

## 19 Causal dynamical triangulation

[398]

## 20 Group field theory

[399, 400]

## 21 Unimodular gravity

[401]

## 22 Hořava–Lifshitz gravity

[402]



## A Miscellaneous math

## References

- [1] A. Einstein, “Approximative Integration of the Field Equations of Gravitation,” *Sitzungsber. Preuss. Akad. Wiss. Berlin (Math. Phys. )* **1916**, 688-696 (1916)
  - [2] J. Polchinski, “String theory. Vol. 1: An introduction to the bosonic string,” Cambridge University Press, 2007, ISBN 978-0-511-25227-3, 978-0-521-67227-6, 978-0-521-63303-1 [doi:10.1017/CBO9780511816079](https://doi.org/10.1017/CBO9780511816079)
  - [3] J. Polchinski, “String theory. Vol. 2: Superstring theory and beyond,” Cambridge University Press, 2007, ISBN 978-0-511-25228-0, 978-0-521-63304-8, 978-0-521-67228-3 [doi:10.1017/CBO9780511618123](https://doi.org/10.1017/CBO9780511618123)
  - [4] E. Kiritsis, “String Theory in a Nutshell: Second Edition,” Princeton University Press, 2019, ISBN 978-0-691-15579-1, 978-0-691-18896-6 [doi.org/10.2307/j.ctvcv4hd1](https://doi.org/10.2307/j.ctvcv4hd1)
  - [5] C. V. Johnson, “D-Branes,” [doi:10.1017/9781009401371](https://doi.org/10.1017/9781009401371)
  - [6] S. Cecotti, “Introduction to String Theory,” *Theor. Math. Phys.* **9783031365300**, pp. (2023) Springer, 2023, ISBN 978-3-031-36529-4, 978-3-031-36530-0 [doi:10.1007/978-3-031-36530-0](https://doi.org/10.1007/978-3-031-36530-0)
  - [7] P. West, “Introduction to strings and branes,” Cambridge University Press, 2012, ISBN 978-0-521-81747-9, 978-1-139-41529-3, 978-0-521-81747-9 [doi:10.1017/CBO9781139045926](https://doi.org/10.1017/CBO9781139045926)
  - [8] K. Becker, M. Becker and J. H. Schwarz, “String theory and M-theory: A modern introduction,” Cambridge University Press, 2006, ISBN 978-0-511-25486-4, 978-0-521-86069-7, 978-0-511-81608-6 [doi:10.1017/CBO9780511816086](https://doi.org/10.1017/CBO9780511816086)
  - [9] R. Blumenhagen, D. Lüst and S. Theisen, “Basic concepts of string theory,” Springer, 2013, ISBN 978-3-642-29496-9 [doi:10.1007/978-3-642-29497-6](https://doi.org/10.1007/978-3-642-29497-6)
  - [10] L. E. Ibanez and A. M. Uranga, “String theory and particle physics: An introduction to string phenomenology,” Cambridge University Press, 2012, ISBN 978-0-521-51752-2, 978-1-139-22742-1 [doi:10.1017/CBO9781139018951](https://doi.org/10.1017/CBO9781139018951)
  - [11] Pierre Deligne, Pavel Etingof, Daniel S. Freed, Lisa C. Jeffrey, David Kazhdan, John W. Morgan, David R. Morrison, Edward Witten, “Quantum Fields and Strings: A Course for Mathematicians. Vol. 1,” [ias.edu/math/qft](https://ias.edu/math/qft)
  - [12] Pierre Deligne, Pavel Etingof, Daniel S. Freed, Lisa C. Jeffrey, David Kazhdan, John W. Morgan, David R. Morrison, Edward Witten, “Quantum Fields and Strings: A Course for Mathematicians. Vol. 2,” [ias.edu/math/qft](https://ias.edu/math/qft)
  - [13] D. Tong, “Lectures on String Theory,” <http://www.damtp.cam.ac.uk/user/tong/string/string.pdf>
  - [14] H. Erbin, “String Field Theory: A Modern Introduction,” *Lect. Notes Phys.* **980**, 1-421 (2021) 2021, ISBN 978-3-030-65320-0, 978-3-030-65321-7 [doi:10.1007/978-3-030-65321-7](https://doi.org/10.1007/978-3-030-65321-7) [arXiv:2301.01686 [hep-th]]. Latest at <https://harolderbin.com/science-books/>
- 
- [15] S. B. Giddings, “The deepest problem: some perspectives on quantum gravity,” [arXiv:2202.08292 [hep-th]].
  - [16] C. Kiefer, “Quantum Gravity,” Oxford University Press, 2007, ISBN 978-0-19-921252-1 [doi:10.1093/acprof:oso/9780199585205.001.0001](https://doi.org/10.1093/acprof:oso/9780199585205.001.0001)

- [17] D. Oriti, “Approaches to quantum gravity: Toward a new understanding of space, time and matter,” Cambridge University Press, 2009, ISBN 978-0-521-86045-1, 978-0-511-51240-7 doi:[10.1017/CBO9780511575549](https://doi.org/10.1017/CBO9780511575549)
- [18] C. Kiefer, “Quantum gravity - an unfinished revolution,” [[arXiv:2302.13047](https://arxiv.org/abs/2302.13047) [gr-qc]].
- [19] R. Loll, G. Fabiano, D. Frattulillo and F. Wagner, “Quantum Gravity in 30 Questions,” PoS **CORFU2021**, 316 (2022) doi:[10.22323/1.406.0316](https://doi.org/10.22323/1.406.0316) [[arXiv:2206.06762](https://arxiv.org/abs/2206.06762) [hep-th]].
- [20] L. Smolin, “How far are we from the quantum theory of gravity?,” [[arXiv:hep-th/0303185](https://arxiv.org/abs/hep-th/0303185) [hep-th]].
- [21] Luboš Motl, “Diff(M) as a gauge group and local observables in theories with gravity,” Physics Stack Exchange <https://physics.stackexchange.com/a/4360/264772>
- [22] P. Berglund, L. Freidel, T. Hubsch, J. Kowalski-Glikman, R. G. Leigh, D. Mattingly and D. Minic, “Infrared Properties of Quantum Gravity: UV/IR Mixing, Gravitizing the Quantum – Theory and Observation,” [[arXiv:2202.06890](https://arxiv.org/abs/2202.06890) [hep-th]].
- [23] S. B. Giddings, “Holography and unitarity,” JHEP **11**, 056 (2020) doi:[10.1007/JHEP11\(2020\)056](https://doi.org/10.1007/JHEP11(2020)056) [[arXiv:2004.07843](https://arxiv.org/abs/2004.07843) [hep-th]].
- [24] D. Marolf, “Holography without strings?,” Class. Quant. Grav. **31**, 015008 (2014) doi:[10.1088/0264-9381/31/1/015008](https://doi.org/10.1088/0264-9381/31/1/015008) [[arXiv:1308.1977](https://arxiv.org/abs/1308.1977) [hep-th]].
- [25] T. Jacobson and P. Nguyen, “Diffeomorphism invariance and the black hole information paradox,” Phys. Rev. D **100**, no.4, 046002 (2019) doi:[10.1103/PhysRevD.100.046002](https://doi.org/10.1103/PhysRevD.100.046002) [[arXiv:1904.04434](https://arxiv.org/abs/1904.04434) [gr-qc]].
- [26] G. 't Hooft, “Dimensional reduction in quantum gravity,” Conf. Proc. C **930308**, 284-296 (1993) [[arXiv:gr-qc/9310026](https://arxiv.org/abs/gr-qc/9310026) [gr-qc]].
- 
- [27] S. Carlip, D. W. Chiou, W. T. Ni and R. Woodard, “Quantum Gravity: A Brief History of Ideas and Some Prospects,” Int. J. Mod. Phys. D **24**, no.11, 1530028 (2015) doi:[10.1142/S0218271815300281](https://doi.org/10.1142/S0218271815300281) [[arXiv:1507.08194](https://arxiv.org/abs/1507.08194) [gr-qc]].
- [28] P. Di Vecchia, “The Birth of string theory,” Lect. Notes Phys. **737**, 59-118 (2008) [[arXiv:0704.0101](https://arxiv.org/abs/0704.0101) [hep-th]].
- [29] J. H. Schwarz, “The Early History of String Theory and Supersymmetry,” [[arXiv:1201.0981](https://arxiv.org/abs/1201.0981) [physics.hist-ph]].
- [30] S. Mukhi, “String theory: a perspective over the last 25 years,” Class. Quant. Grav. **28**, 153001 (2011) doi:[10.1088/0264-9381/28/15/153001](https://doi.org/10.1088/0264-9381/28/15/153001) [[arXiv:1110.2569](https://arxiv.org/abs/1110.2569) [physics.pop-ph]].
- [31] J. Polchinski, “Memories of a Theoretical Physicist,” MIT Press, 2022, ISBN 978-0-262-54344-6, 978-0-262-36890-2 [[arXiv:1708.09093](https://arxiv.org/abs/1708.09093) [physics.hist-ph]].
- [32] J. Polchinski, “Dualities of Fields and Strings,” Stud. Hist. Phil. Sci. B **59**, 6-20 (2017) doi:[10.1016/j.shpsb.2015.08.011](https://doi.org/10.1016/j.shpsb.2015.08.011) [[arXiv:1412.5704](https://arxiv.org/abs/1412.5704) [hep-th]].
- [33] M. J. Duff, “M-history without the M,” Contemp. Phys. **57**, 83 (2016) doi:[10.1080/00107514.2014.992964](https://doi.org/10.1080/00107514.2014.992964) [[arXiv:1501.04098](https://arxiv.org/abs/1501.04098) [physics.hist-ph]].
- [34] C. Rovelli, “Notes for a brief history of quantum gravity,” [[arXiv:gr-qc/0006061](https://arxiv.org/abs/gr-qc/0006061) [gr-qc]].
- [35] W. Siegel, “Particles, Strings, & Other Things,” [insti.physics.sunysb.edu/~siegel/PSOT.pdf](https://insti.physics.sunysb.edu/~siegel/PSOT.pdf)
- [36] S. Deser, “Forks in the Road A Life in Physics,” doi:[10.1142/12205](https://doi.org/10.1142/12205)

- 
- [37] T. Jacobson, “Introduction to quantum fields in curved space-time and the Hawking effect,” doi:10.1007/0-387-24992-3\_2 [[arXiv:gr-qc/0308048](#) [[gr-qc](#)]].
- [38] S. Hollands and R. M. Wald, “Quantum fields in curved spacetime,” *Phys. Rept.* **574**, 1-35 (2015) doi:10.1016/j.physrep.2015.02.001 [[arXiv:1401.2026](#) [[gr-qc](#)]].
- [39] S. Carlip, “Black Hole Thermodynamics,” *Int. J. Mod. Phys. D* **23**, 1430023 (2014) doi:10.1142/S0218271814300237 [[arXiv:1410.1486](#) [[gr-qc](#)]].
- [40] T. Jacobson, “Introductory Lectures on Black Hole Thermodynamics,” [physics.umd.edu/grt/taj/776b/lectures.pdf](#)
- [41] D. Marolf, “The Black Hole information problem: past, present, and future,” *Rept. Prog. Phys.* **80**, no.9, 092001 (2017) doi:10.1088/1361-6633/aa77cc [[arXiv:1703.02143](#) [[gr-qc](#)]].
- [42] T. Hartman, “Lectures on Quantum Gravity and Black Holes,” [hartmanhep.net/topics2015/gravity-lectures.pdf](#)
- [43] D. Harlow, “Jerusalem Lectures on Black Holes and Quantum Information,” *Rev. Mod. Phys.* **88**, 015002 (2016) doi:10.1103/RevModPhys.88.015002 [[arXiv:1409.1231](#) [[hep-th](#)]].
- [44] S. D. Mathur, “What the information paradox is not,” [[arXiv:1108.0302](#) [[hep-th](#)]].
- [45] S. D. Mathur, “The Information paradox: A Pedagogical introduction,” *Class. Quant. Grav.* **26**, 224001 (2009) doi:10.1088/0264-9381/26/22/224001 [[arXiv:0909.1038](#) [[hep-th](#)]].
- [46] S. D. Mathur, “What Exactly is the Information Paradox?,” *Lect. Notes Phys.* **769**, 3-48 (2009) doi:10.1007/978-3-540-88460-6\_1 [[arXiv:0803.2030](#) [[hep-th](#)]].
- [47] P. H. Lambert, “Introduction to Black Hole Evaporation,” *PoS Modave2013*, 001 (2013) doi:10.22323/1.201.0001 [[arXiv:1310.8312](#) [[gr-qc](#)]].
- [48] J. Polchinski, “The Black Hole Information Problem,” doi:10.1142/9789813149441\_0006 [[arXiv:1609.04036](#) [[hep-th](#)]].
- [49] A. Almheiri, T. Hartman, J. Maldacena, E. Shaghoulian and A. Tajdini, “The entropy of Hawking radiation,” *Rev. Mod. Phys.* **93**, no.3, 035002 (2021) doi:10.1103/RevModPhys.93.035002 [[arXiv:2006.06872](#) [[hep-th](#)]].
- [50] J. Kaplan, [sites.krieger.jhu.edu/jared-kaplan/files/2020/01/QuantumGravityLectureNotes.pdf](#)
- [51] D. N. Page, “Hawking radiation and black hole thermodynamics,” *New J. Phys.* **7**, 203 (2005) doi:10.1088/1367-2630/7/1/203 [[arXiv:hep-th/0409024](#) [[hep-th](#)]].
- [52] J. H. Traschen, “An Introduction to black hole evaporation,” [[arXiv:gr-qc/0010055](#) [[gr-qc](#)]].
- [53] A. C. Wall, “A Survey of Black Hole Thermodynamics,” [[arXiv:1804.10610](#) [[gr-qc](#)]].
- [54] S. Raju, “Lessons from the information paradox,” *Phys. Rept.* **943**, 1-80 (2022) doi:10.1016/j.physrep.2021.10.001 [[arXiv:2012.05770](#) [[hep-th](#)]].
- [55] B. S. Kay, “Quantum Field Theory in Curved Spacetime (2nd Edition),” [[arXiv:2308.14517](#) [[gr-qc](#)]].
- 
- [56] J. F. Donoghue, “Quantum General Relativity and Effective Field Theory,” doi:10.1007/978-981-19-3079-9\_1-1 [[arXiv:2211.09902](#) [[hep-th](#)]].

- [57] A. Rocci and T. Van Riet, “The Quantum Theory Of Gravitation, Effective Field Theories, and Strings: Yesterday And Today,” [[arXiv:2403.14008](#) [[physics.hist-ph](#)]].
- [58] C. P. Burgess, “Quantum gravity in everyday life: General relativity as an effective field theory,” *Living Rev. Rel.* **7**, 5-56 (2004) doi:10.12942/lrr-2004-5 [[arXiv:gr-qc/0311082](#) [[gr-qc](#)]].
- [59] C. P. Burgess, “Introduction to Effective Field Theory,” Cambridge University Press, 2020, ISBN 978-1-139-04804-0, 978-0-521-19547-8 doi:10.1017/9781139048040
- [60] J. F. Donoghue and G. Menezes, “Causality and gravity,” *JHEP* **11**, 010 (2021) doi:10.1007/JHEP11(2021)010 [[arXiv:2106.05912](#) [[hep-th](#)]].
- [61] J. Polchinski, “String theory to the rescue,” [[arXiv:1512.02477](#) [[hep-th](#)]].
- [62] J. Polchinski, “Why trust a theory? Some further remarks (part 1),” [[arXiv:1601.06145](#) [[hep-th](#)]].
- [63] J. Conlon, “Why string theory?,” CRC Pr., 2016, ISBN 978-1-4822-4247-8 doi:10.1201/9781315272368
- 
- [64] J. D. Qualls, “Lectures on Conformal Field Theory,” [[arXiv:1511.04074](#) [[hep-th](#)]].
- [65] A. N. Schellekens, <https://www.nikhef.nl/~t58/CFT.pdf>
- [66] R. Blumenhagen and E. Plauschinn, “Introduction to conformal field theory: with applications to String theory,” *Lect. Notes Phys.* **779**, 1-256 (2009) doi:10.1007/978-3-642-00450-6
- [67] M. Gillioz, “Conformal field theory for particle physicists,” Springer, 2023, ISBN 978-3-031-27085-7, 978-3-031-27086-4 doi:10.1007/978-3-031-27086-4 [[arXiv:2207.09474](#) [[hep-th](#)]].
- [68] S. Rychkov, “EPFL Lectures on Conformal Field Theory in  $D \geq 3$  Dimensions,” doi:10.1007/978-3-319-43626-5 [[arXiv:1601.05000](#) [[hep-th](#)]].
- [69] D. Simmons-Duffin, <https://github.com/davidsd/ph229/blob/master/ph229-notes.pdf>
- [70] S. Nawata, R. Tao and D. Yokoyama, “Fudan lectures on 2d conformal field theory,” [[arXiv:2208.05180](#) [[hep-th](#)]].
- [71] A. M. Evans, A. Miller and A. Russell, “A Conformal Field Theory Primer in  $D \geq 3$ ,” [[arXiv:2309.10107](#) [[hep-th](#)]].
- [72] Y. Nakayama, “Scale invariance vs conformal invariance,” *Phys. Rept.* **569**, 1-93 (2015) doi:10.1016/j.physrep.2014.12.003 [[arXiv:1302.0884](#) [[hep-th](#)]].
- [73] G. M. Shore, “The c and a-theorems and the Local Renormalisation Group,” Springer, 2017, ISBN 978-3-319-53999-7, 978-3-319-54000-9 doi:10.1007/978-3-319-54000-9 [[arXiv:1601.06662](#) [[hep-th](#)]].
- [74] S. S. Pufu, “The F-Theorem and F-Maximization,” *J. Phys. A* **50**, no.44, 443008 (2017) doi:10.1088/1751-8121/aa6765 [[arXiv:1608.02960](#) [[hep-th](#)]].
- [75] T. Hartman, D. Mazac, D. Simmons-Duffin and A. Zhiboedov, “Snowmass White Paper: The Analytic Conformal Bootstrap,” [[arXiv:2202.11012](#) [[hep-th](#)]].
- [76] J. Henriksson, “Analytic bootstrap for perturbative conformal field theories,” [[arXiv:2008.12600](#) [[hep-th](#)]].

- [77] D. Poland and D. Simmons-Duffin, “Snowmass White Paper: The Numerical Conformal Bootstrap,” [[arXiv:2203.08117 \[hep-th\]](#)].
- [78] S. M. Chester, “Weizmann lectures on the numerical conformal bootstrap,” *Phys. Rept.* **1045**, 1-44 (2023) doi:10.1016/j.physrep.2023.10.008 [[arXiv:1907.05147 \[hep-th\]](#)].
- [79] D. Gaiotto and X. Yin, “Notes on superconformal Chern-Simons-Matter theories,” *JHEP* **08**, 056 (2007) doi:10.1088/1126-6708/2007/08/056 [[arXiv:0704.3740 \[hep-th\]](#)].
- [80] J. A. Minahan, “Review of AdS/CFT Integrability, Chapter I.1: Spin Chains in N=4 Super Yang-Mills,” *Lett. Math. Phys.* **99**, 33-58 (2012) doi:10.1007/s11005-011-0522-9 [[arXiv:1012.3983 \[hep-th\]](#)].
- [81] M. Aghand, G. Arias-Tamargo, A. Mininno, H. Y. Sun, Z. Sun, Y. Wang and F. Xu, “The hitchhiker’s guide to 4d  $\mathcal{N} = 2$  superconformal field theories,” *SciPost Phys. Lect. Notes* **64**, 1 (2022) doi:10.21468/SciPostPhysLectNotes.64 [[arXiv:2112.14764 \[hep-th\]](#)].
- [82] Y. Tachikawa, “Lectures on 4d N=1 dynamics and related topics,” [[arXiv:1812.08946 \[hep-th\]](#)].
- [83] J. J. Heckman and T. Rudelius, “Top Down Approach to 6D SCFTs,” *J. Phys. A* **52**, no.9, 093001 (2019) doi:10.1088/1751-8121/aafc81 [[arXiv:1805.06467 \[hep-th\]](#)].
- [84] M. Schottenloher, “A mathematical introduction to conformal field theory,” *Lect. Notes Phys.* **759**, 1-237 (2008) doi:10.1007/978-3-540-68628-6
- [85] P. Kravchuk, J. Qiao and S. Rychkov, “Distributions in CFT. Part I. Cross-ratio space,” *JHEP* **05**, 137 (2020) doi:10.1007/JHEP05(2020)137 [[arXiv:2001.08778 \[hep-th\]](#)].
- [86] P. Kravchuk, J. Qiao and S. Rychkov, “Distributions in CFT. Part II. Minkowski space,” *JHEP* **08**, 094 (2021) doi:10.1007/JHEP08(2021)094 [[arXiv:2104.02090 \[hep-th\]](#)].
- 
- [87] D. Tong, “Lectures on Supersymmetric Quantum Mechanics,” <http://www.damtp.cam.ac.uk/user/tong/susyqm.html>
- [88] David Skinner, “Supersymmetry,” <http://www.damtp.cam.ac.uk/user/dbs26/SUSY.html>
- [89] D. Tong, “Lectures on Supersymmetry,” <http://www.damtp.cam.ac.uk/user/tong/susy.html>
- [90] M. Bertolini, <https://people.sissa.it/~bertmat/teaching.htm>
- [91] D. S. Freed, “Five lectures on supersymmetry,” AMS, 1999, ISBN 978-0-8218-1953-1 [bookstore.ams.org/FLS](http://bookstore.ams.org/FLS)
- [92] K. A. Intriligator and N. Seiberg, “Lectures on supersymmetric gauge theories and electric-magnetic duality,” *Nucl. Phys. B Proc. Suppl.* **45BC**, 1-28 (1996) doi:10.1016/0920-5632(95)00626-5 [[arXiv:hep-th/9509066 \[hep-th\]](#)].
- [93] D. S. Berman and E. Rabinovici, “Supersymmetric gauge theories,” [[arXiv:hep-th/0210044 \[hep-th\]](#)].
- [94] S. S. Razamat, E. Sabag, O. Sela and G. Zafrir, “Aspects of 4d supersymmetric dynamics and geometry,” *SciPost Phys. Lect. Notes* **78**, 1 (2024) doi:10.21468/SciPostPhysLectNotes.78 [[arXiv:2203.06880 \[hep-th\]](#)].
- [95] D. Bertolini, J. Thaler and Z. Thomas, “Super-Tricks for Superspace,” doi:10.1142/9789814525220\_0009 [[arXiv:1302.6229 \[hep-ph\]](#)].

- [96] D. Z. Freedman and A. Van Proeyen, “Supergravity,” Cambridge Univ. Press, 2012, ISBN 978-1-139-36806-3, 978-0-521-19401-3 doi:[10.1017/CBO9781139026833](https://doi.org/10.1017/CBO9781139026833)
- [97] H. Nastase, “Introduction to Supergravity,” [[arXiv:1112.3502](https://arxiv.org/abs/1112.3502) [hep-th]].
- [98] E. Sezgin, “Survey of supergravities,” [[arXiv:2312.06754](https://arxiv.org/abs/2312.06754) [hep-th]].
- [99] H. Samtleben, “11D Supergravity and Hidden Symmetries,” doi:[10.1007/978-981-19-3079-9\\_45-1](https://doi.org/10.1007/978-981-19-3079-9_45-1) [[arXiv:2303.12682](https://arxiv.org/abs/2303.12682) [hep-th]].
- [100] A. Miemiec and I. Schnakenburg, “Basics of M-theory,” Fortsch. Phys. **54**, 5-72 (2006) doi:[10.1002/prop.200510256](https://doi.org/10.1002/prop.200510256) [[arXiv:hep-th/0509137](https://arxiv.org/abs/hep-th/0509137) [hep-th]].
- [101] B. de Wit, “Supergravity,” [[arXiv:hep-th/0212245](https://arxiv.org/abs/hep-th/0212245) [hep-th]].
- [102] W. Taylor, “TASI Lectures on Supergravity and String Vacua in Various Dimensions,” [[arXiv:1104.2051](https://arxiv.org/abs/1104.2051) [hep-th]].
- [103] M. Trigiante, “Gauged Supergravities,” Phys. Rept. **680**, 1-175 (2017) doi:[10.1016/j.physrep.2017.03.001](https://doi.org/10.1016/j.physrep.2017.03.001) [[arXiv:1609.09745](https://arxiv.org/abs/1609.09745) [hep-th]].
- [104] A. Gallerati, “Constructing black hole solutions in supergravity theories,” Int. J. Mod. Phys. A **34**, no.35, 1930017 (2020) doi:[10.1142/S0217751X19300175](https://doi.org/10.1142/S0217751X19300175) [[arXiv:1905.04104](https://arxiv.org/abs/1905.04104) [hep-th]].
- [105] A. Sen, “Ultraviolet and Infrared Divergences in Superstring Theory,” [[arXiv:1512.00026](https://arxiv.org/abs/1512.00026) [hep-th]].
- [106] N. Berkovits, “Perturbative finiteness of superstring theory,” PoS **WC2004**, 009 (2004) doi:[10.22323/1.013.0009](https://doi.org/10.22323/1.013.0009)
- [107] O. Hohm, D. Lüst and B. Zwiebach, “The Spacetime of Double Field Theory: Review, Remarks, and Outlook,” Fortsch. Phys. **61**, 926-966 (2013) doi:[10.1002/prop.201300024](https://doi.org/10.1002/prop.201300024) [[arXiv:1309.2977](https://arxiv.org/abs/1309.2977) [hep-th]].
- [108] D. S. Berman and D. C. Thompson, “Duality Symmetric String and M-Theory,” Phys. Rept. **566**, 1-60 (2014) doi:[10.1016/j.physrep.2014.11.007](https://doi.org/10.1016/j.physrep.2014.11.007) [[arXiv:1306.2643](https://arxiv.org/abs/1306.2643) [hep-th]].
- [109] G. Aldazabal, D. Marques and C. Nunez, “Double Field Theory: A Pedagogical Review,” Class. Quant. Grav. **30**, 163001 (2013) doi:[10.1088/0264-9381/30/16/163001](https://doi.org/10.1088/0264-9381/30/16/163001) [[arXiv:1305.1907](https://arxiv.org/abs/1305.1907) [hep-th]].
- [110] T. Weigand, “TASI Lectures on F-theory,” PoS **TASI2017**, 016 (2018) [[arXiv:1806.01854](https://arxiv.org/abs/1806.01854) [hep-th]].
- 
- [111] T. Van Riet and G. Zoccarato, “Beginners lectures on flux compactifications and related Swampland topics,” Phys. Rept. **1049**, 1-51 (2024) doi:[10.1016/j.physrep.2023.11.003](https://doi.org/10.1016/j.physrep.2023.11.003) [[arXiv:2305.01722](https://arxiv.org/abs/2305.01722) [hep-th]].
- [112] L. B. Anderson and M. Karkheiran, “TASI Lectures on Geometric Tools for String Compactifications,” PoS **TASI2017**, 013 (2018) doi:[10.22323/1.305.0013](https://doi.org/10.22323/1.305.0013) [[arXiv:1804.08792](https://arxiv.org/abs/1804.08792) [hep-th]].
- [113] L. McAllister and F. Quevedo, “Moduli Stabilization in String Theory,” [[arXiv:2310.20559](https://arxiv.org/abs/2310.20559) [hep-th]].
- [114] M. Grana, “Flux compactifications in string theory: A Comprehensive review,” Phys. Rept. **423**, 91-158 (2006) doi:[10.1016/j.physrep.2005.10.008](https://doi.org/10.1016/j.physrep.2005.10.008) [[arXiv:hep-th/0509003](https://arxiv.org/abs/hep-th/0509003) [hep-th]].



- [115] M. R. Douglas and S. Kachru, “Flux compactification,” *Rev. Mod. Phys.* **79**, 733-796 (2007) doi:10.1103/RevModPhys.79.733 [arXiv:hep-th/0610102 [hep-th]].
- [116] A. Font and S. Theisen, “Introduction to string compactification,” *Lect. Notes Phys.* **668**, 101-181 (2005) 10.1007/11374060\_3
- [117] S. Alexandrov, “Twistor Approach to String Compactifications: a Review,” *Phys. Rept.* **522**, 1-57 (2013) doi:10.1016/j.physrep.2012.09.005 [arXiv:1111.2892 [hep-th]].
- [118] E. Plauschinn, “Non-geometric backgrounds in string theory,” *Phys. Rept.* **798**, 1-122 (2019) doi:10.1016/j.physrep.2018.12.002 [arXiv:1811.11203 [hep-th]].
- [119] B. Wecht, “Lectures on Nongeometric Flux Compactifications,” *Class. Quant. Grav.* **24**, S773-S794 (2007) doi:10.1088/0264-9381/24/21/S03 [arXiv:0708.3984 [hep-th]].
- [120] Y. Kimura, “Eight-dimensional non-geometric heterotic strings and enhanced gauge groups,” *Eur. Phys. J. ST* **232**, no.23-24, 3697-3704 (2023) doi:10.1140/epjs/s11734-023-00889-3 [arXiv:2305.09240 [hep-th]].
- [121] M. Cicoli, J. P. Conlon, A. Maharana, S. Parameswaran, F. Quevedo and I. Zavala, “String cosmology: From the early universe to today,” *Phys. Rept.* **1059**, 1-155 (2024) doi:10.1016/j.physrep.2024.01.002 [arXiv:2303.04819 [hep-th]].
- [122] G. K. Leontaris and P. Shukla, “Seeking de Sitter vacua in the string landscape,” *PoS CORFU2022*, 058 (2023) doi:10.22323/1.436.0058 [arXiv:2303.16689 [hep-th]].
- [123] P. Berglund, T. Hübsch and D. Minic, “On de Sitter Spacetime and String Theory,” *Int. J. Mod. Phys. D* **32**, 2330002 (2023) doi:10.1142/S0218271823300021 [arXiv:2212.06086 [hep-th]].
- [124] D. Baumann and L. McAllister, “Inflation and String Theory,” Cambridge University Press, 2015, ISBN 978-1-107-08969-3, 978-1-316-23718-2 doi:10.1017/CBO9781316105733 [arXiv:1404.2601 [hep-th]].
- [125] D. Baumann, “Inflation,” doi:10.1142/9789814327183-0010 [arXiv:0907.5424 [hep-th]].
- [126] J. Polchinski, “The Cosmological Constant and the String Landscape,” [arXiv:hep-th/0603249 [hep-th]].
- [127] R. Bousso, “TASI Lectures on the Cosmological Constant,” *Gen. Rel. Grav.* **40**, 607-637 (2008) doi:10.1007/s10714-007-0557-5 [arXiv:0708.4231 [hep-th]].
- [128] E. Silverstein, “TASI lectures on cosmological observables and string theory,” doi:10.1142/9789813149441-0009 [arXiv:1606.03640 [hep-th]].
- [129] R. Brandenberger, “Superstring cosmology — a complementary review,” *JCAP* **11**, 019 (2023) doi:10.1088/1475-7516/2023/11/019 [arXiv:2306.12458 [hep-th]].
- [130] J. Erdmenger, “String cosmology: Modern string theory concepts from the Big Bang to cosmic structure,” doi:10.1002/9783527628063
- [131] F. Marchesano, G. Shiu and T. Weigand, “The Standard Model from String Theory: What Have We Learned?,” doi:10.1146/annurev-nucl-102622-01223 [arXiv:2401.01939 [hep-th]].
- [132] M. Cvetič, J. Halverson, G. Shiu and W. Taylor, “Snowmass White Paper: String Theory and Particle Physics,” [arXiv:2204.01742 [hep-th]].
- [133] F. Marchesano, B. Schellekens and T. Weigand, “D-brane and F-theory Model Building,” [arXiv:2212.07443 [hep-th]].



- [134] A. Arvanitaki, S. Dimopoulos, S. Dubovsky, N. Kaloper and J. March-Russell, “String Axiverse,” *Phys. Rev. D* **81**, 123530 (2010) doi:10.1103/PhysRevD.81.123530 [[arXiv:0905.4720 \[hep-th\]](#)].
- [135] M. Reece, “TASI Lectures: (No) Global Symmetries to Axion Physics,” *PoS TASI2022*, 008 (2024) doi:10.22323/1.439.0008 [[arXiv:2304.08512 \[hep-ph\]](#)].
- 
- [136] N. B. Agmon, A. Bedroya, M. J. Kang and C. Vafa, “Lectures on the string landscape and the Swampland,” [[arXiv:2212.06187 \[hep-th\]](#)].
- [137] E. Palti, “The Swampland: Introduction and Review,” *Fortsch. Phys.* **67**, no.6, 1900037 (2019) doi:10.1002/prop.201900037 [[arXiv:1903.06239 \[hep-th\]](#)].
- [138] T. D. Brennan, F. Carta and C. Vafa, “The String Landscape, the Swampland, and the Missing Corner,” *PoS TASI2017*, 015 (2017) doi:10.22323/1.305.0015 [[arXiv:1711.00864 \[hep-th\]](#)].
- [139] M. van Beest, J. Calderón-Infante, D. Mirfendereski and I. Valenzuela, “Lectures on the Swampland Program in String Compactifications,” *Phys. Rept.* **989**, 1-50 (2022) doi:10.1016/j.physrep.2022.09.002 [[arXiv:2102.01111 \[hep-th\]](#)].
- [140] M. Graña and A. Herráez, “The Swampland Conjectures: A Bridge from Quantum Gravity to Particle Physics,” *Universe* **7**, no.8, 273 (2021) doi:10.3390/universe7080273 [[arXiv:2107.00087 \[hep-th\]](#)].
- [141] K. Hashimoto, “D-brane: Superstrings and new perspective of our world,” Springer, 2012, ISBN 978-3-642-23573-3 doi:10.1007/978-3-642-23574-0
- [142] C. Bachas, “D-branes,” [[arXiv:2311.18456 \[hep-th\]](#)].
- 
- [143] O. Aharony, S. S. Gubser, J. M. Maldacena, H. Ooguri and Y. Oz, “Large N field theories, string theory and gravity,” *Phys. Rept.* **323**, 183-386 (2000) doi:10.1016/S0370-1573(99)00083-6 [[arXiv:hep-th/9905111 \[hep-th\]](#)].
- [144] H. Nastase, “Introduction to the ADS/CFT Correspondence,” Cambridge University Press, 2015, ISBN 978-1-107-08585-5, 978-1-316-35530-5 doi:10.1017/CBO9781316090954
- [145] M. Ammon and J. Erdmenger, “Gauge/gravity duality: Foundations and applications,” Cambridge University Press, 2015, ISBN 978-1-107-01034-5, 978-1-316-23594-2 doi:10.1017/CBO9780511846373
- [146] J. Polchinski, “Introduction to Gauge/Gravity Duality,” doi:10.1142/9789814350525\_0001 [[arXiv:1010.6134 \[hep-th\]](#)].
- [147] J. Kaplan,  
[sites.krieger.jhu.edu/jared-kaplan/files/2016/05/AdSCFTCourseNotesCurrentPublic.pdf](https://sites.krieger.jhu.edu/jared-kaplan/files/2016/05/AdSCFTCourseNotesCurrentPublic.pdf)
- [148] O. DeWolfe, “TASI Lectures on Applications of Gauge/Gravity Duality,” *PoS TASI2017*, 014 (2018) doi:10.22323/1.305.0014 [[arXiv:1802.08267 \[hep-th\]](#)].
- [149] S. De Haro, D. R. Mayerson and J. N. Butterfield, “Conceptual Aspects of Gauge/Gravity Duality,” *Found. Phys.* **46**, no.11, 1381-1425 (2016) doi:10.1007/s10701-016-0037-4 [[arXiv:1509.09231 \[physics.hist-ph\]](#)].
- [150] V. E. Hubeny, “The AdS/CFT Correspondence,” *Class. Quant. Grav.* **32**, no.12, 124010 (2015) doi:10.1088/0264-9381/32/12/124010 [[arXiv:1501.00007 \[gr-qc\]](#)].

- [151] D. Tong, “TASI lectures on solitons: Instantons, monopoles, vortices and kinks,” [[arXiv:hep-th/0509216](#) [hep-th]].
- [152] P. Kraus, “Lectures on black holes and the AdS(3) / CFT(2) correspondence,” *Lect. Notes Phys.* **755**, 193-247 (2008) [[arXiv:hep-th/0609074](#) [hep-th]].
- [153] C. T. Ma, “AdS<sub>3</sub> Einstein gravity and boundary description: pedagogical review,” *Class. Quant. Grav.* **41**, no.2, 023001 (2024) doi:10.1088/1361-6382/ad17f0 [[arXiv:2310.04665](#) [hep-th]].
- [154] N. Beisert, C. Ahn, L. F. Alday, Z. Bajnok, J. M. Drummond, L. Freyhult, N. Gromov, R. A. Janik, V. Kazakov and T. Klose, *et al.* “Review of AdS/CFT Integrability: An Overview,” *Lett. Math. Phys.* **99**, 3-32 (2012) doi:10.1007/s11005-011-0529-2 [[arXiv:1012.3982](#) [hep-th]].
- [155] S. Giombi, “Higher Spin CFT Duality,” doi:10.1142/9789813149441\_0003 [[arXiv:1607.02967](#) [hep-th]].
- [156] Andrea Campoleoni and Stefan Fredenhagen, “Higher-spin gauge theories in three spacetime dimensions,” [[arXiv:2403.16567](#) [hep-th]].
- [157] X. Bekaert, N. Boulanger, A. Campoleoni, M. Chiodaroli, D. Francia, M. Grigoriev, E. Sezgin and E. Skvortsov, “Snowmass White Paper: Higher Spin Gravity and Higher Spin Symmetry,” [[arXiv:2205.01567](#) [hep-th]].
- [158] R. Rahman and M. Taronna, “From Higher Spins to Strings: A Primer,” [[arXiv:1512.07932](#) [hep-th]].
- [159] A. Sagnotti, “Notes on Strings and Higher Spins,” *J. Phys. A* **46**, 214006 (2013) doi:10.1088/1751-8113/46/21/214006 [[arXiv:1112.4285](#) [hep-th]].
- [160] V. E. Hubeny, S. Minwalla and M. Rangamani, “The fluid/gravity correspondence,” [[arXiv:1107.5780](#) [hep-th]].
- 
- [161] B. Chen, B. Czech and Z. z. Wang, “Quantum information in holographic duality,” *Rept. Prog. Phys.* **85**, no.4, 046001 (2022) doi:10.1088/1361-6633/ac51b5 [[arXiv:2108.09188](#) [hep-th]].
- [162] M. Headrick, “Lectures on entanglement entropy in field theory and holography,” [[arXiv:1907.08126](#) [hep-th]].
- [163] M. Rangamani and T. Takayanagi, “Holographic Entanglement Entropy,” *Lect. Notes Phys.* **931**, pp.1-246 (2017) Springer, 2017, doi:10.1007/978-3-319-52573-0 [[arXiv:1609.01287](#) [hep-th]].
- [164] N. Callebaut, “Entanglement in Conformal Field Theory and Holography,” *Lect. Notes Phys.* **1022**, 239-271 (2023) doi:10.1007/978-3-031-42096-2\_10 [[arXiv:2303.16827](#) [hep-th]].
- [165] T. Nishioka, “Entanglement entropy: holography and renormalization group,” *Rev. Mod. Phys.* **90**, no.3, 035007 (2018) doi:10.1103/RevModPhys.90.035007 [[arXiv:1801.10352](#) [hep-th]].
- [166] E. Witten, “APS Medal for Exceptional Achievement in Research: Invited article on entanglement properties of quantum field theory,” *Rev. Mod. Phys.* **90**, no.4, 045003 (2018) doi:10.1103/RevModPhys.90.045003 [[arXiv:1803.04993](#) [hep-th]].

- [167] A. Lewkowycz and J. Maldacena, “Generalized gravitational entropy,” *JHEP* **08**, 090 (2013) doi:10.1007/JHEP08(2013)090 [[arXiv:1304.4926 \[hep-th\]](#)].
- [168] X. Dong, A. Lewkowycz and M. Rangamani, “Deriving covariant holographic entanglement,” *JHEP* **11**, 028 (2016) doi:10.1007/JHEP11(2016)028 [[arXiv:1607.07506 \[hep-th\]](#)].
- [169] X. Dong and A. Lewkowycz, “Entropy, Extremality, Euclidean Variations, and the Equations of Motion,” *JHEP* **01**, 081 (2018) doi:10.1007/JHEP01(2018)081 [[arXiv:1705.08453 \[hep-th\]](#)].
- [170] H. Geng, A. Karch, C. Perez-Pardavila, S. Raju, L. Randall, M. Riojas and S. Shashi, “Inconsistency of islands in theories with long-range gravity,” *JHEP* **01**, 182 (2022) doi:10.1007/JHEP01(2022)182 [[arXiv:2107.03390 \[hep-th\]](#)].
- [171] E. J. Martinec, “Trouble in Paradox,” [[arXiv:2203.04947 \[hep-th\]](#)].
- [172] B. Guo, M. R. R. Hughes, S. D. Mathur and M. Mehta, “Contrasting the fuzzball and wormhole paradigms for black holes,” *Turk. J. Phys.* **45**, no.6, 281-365 (2021) doi:10.3906/fiz-2111-13 [[arXiv:2111.05295 \[hep-th\]](#)].
- [173] I. Bena, E. J. Martinec, S. D. Mathur and N. P. Warner, “Fuzzballs and Microstate Geometries: Black-Hole Structure in String Theory,” [[arXiv:2204.13113 \[hep-th\]](#)].
- [174] N. Engelhardt and S. Fischetti, “Surface Theory: the Classical, the Quantum, and the Holographic,” *Class. Quant. Grav.* **36**, no.20, 205002 (2019) doi:10.1088/1361-6382/ab3bda [[arXiv:1904.08423 \[hep-th\]](#)].
- [175] A. Jahn and J. Eisert, “Holographic tensor network models and quantum error correction: a topical review,” *Quantum Sci. Technol.* **6**, no.3, 033002 (2021) doi:10.1088/2058-9565/ac0293 [[arXiv:2102.02619 \[quant-ph\]](#)].
- [176] T. Kibe, P. Mandayam and A. Mukhopadhyay, “Holographic spacetime, black holes and quantum error correcting codes: a review,” *Eur. Phys. J. C* **82**, no.5, 463 (2022) doi:10.1140/epjc/s10052-022-10382-1 [[arXiv:2110.14669 \[hep-th\]](#)].
- [177] D. Harlow, “TASI Lectures on the Emergence of Bulk Physics in AdS/CFT,” *PoS TASI2017*, 002 (2018) doi:10.22323/1.305.0002 [[arXiv:1802.01040 \[hep-th\]](#)].
- [178] V. Jahnke, “Recent developments in the holographic description of quantum chaos,” *Adv. High Energy Phys.* **2019**, 9632708 (2019) doi:10.1155/2019/9632708 [[arXiv:1811.06949 \[hep-th\]](#)].
- [179] P. Saad, “TASI lectures on random matrix universality in AdS/CFT,” *PoS TASI2021*, 011 (2023) doi:10.22323/1.403.0011
- [180] A. Bhattacharyya, L. K. Joshi and B. Sundar, “Quantum information scrambling: from holography to quantum simulators,” *Eur. Phys. J. C* **82**, no.5, 458 (2022) doi:10.1140/epjc/s10052-022-10377-y [[arXiv:2111.11945 \[hep-th\]](#)].
- [181] L. Susskind, “Three Lectures on Complexity and Black Holes,” Springer, 2020, ISBN 978-3-030-45108-0, 978-3-030-45109-7 doi:10.1007/978-3-030-45109-7 [[arXiv:1810.11563 \[hep-th\]](#)].
- [182] S. Aaronson, “The Complexity of Quantum States and Transformations: From Quantum Money to Black Holes,” [[arXiv:1607.05256 \[quant-ph\]](#)].

- [183] T. G. Mertens and G. J. Turiaci, “Solvable models of quantum black holes: a review on Jackiw–Teitelboim gravity,” *Living Rev. Rel.* **26**, no.1, 4 (2023) doi:10.1007/s41114-023-00046-1 [[arXiv:2210.10846](#) [[hep-th](#)]].
- [184] G. Sárosi, “AdS<sub>2</sub> holography and the SYK model,” *PoS Modave2017*, 001 (2018) doi:10.22323/1.323.0001 [[arXiv:1711.08482](#) [[hep-th](#)]].
- [185] D. A. Trunin, “Pedagogical introduction to the Sachdev–Ye–Kitaev model and two-dimensional dilaton gravity,” *Usp. Fiz. Nauk* **191**, no.3, 225-261 (2021) doi:10.3367/UFNe.2020.06.038805 [[arXiv:2002.12187](#) [[hep-th](#)]].
- [186] M. Berkooz, M. Isachenkov, V. Narovlansky and G. Torrents, “Towards a full solution of the large N double-scaled SYK model,” *JHEP* **03**, 079 (2019) doi:10.1007/JHEP03(2019)079 [[arXiv:1811.02584](#) [[hep-th](#)]].
- [187] J. Sorce, “Notes on the type classification of von Neumann algebras,” *Rev. Math. Phys.* **36**, no.02, 2430002 (2024) doi:10.1142/S0129055X24300024 [[arXiv:2302.01958](#) [[hep-th](#)]].
- [188] E. Witten, “Algebras, Regions, and Observers,” [[arXiv:2303.02837](#) [[hep-th](#)]].
- [189] S. Hollands, “GGI Lectures on Entropy, Operator Algebras and Black Holes,” [[arXiv:2209.05132](#) [[hep-th](#)]].
- [190] F. Hiai, “Concise lectures on selected topics of von Neumann algebras,” [[arXiv:2004.02383](#) [[math.OA](#)]].
- 
- [191] L. Donnay, “Celestial holography: An asymptotic symmetry perspective,” [[arXiv:2310.12922](#) [[hep-th](#)]].
- [192] A. Strominger, “Lectures on the Infrared Structure of Gravity and Gauge Theory,” [[arXiv:1703.05448](#) [[hep-th](#)]].
- [193] S. Pasterski, M. Pate and A. M. Raclariu, “Celestial Holography,” [[arXiv:2111.11392](#) [[hep-th](#)]].
- [194] A. M. Raclariu, “Lectures on Celestial Holography,” [[arXiv:2107.02075](#) [[hep-th](#)]].
- [195] S. Pasterski, “Lectures on celestial amplitudes,” *Eur. Phys. J. C* **81**, no.12, 1062 (2021) doi:10.1140/epjc/s10052-021-09846-7 [[arXiv:2108.04801](#) [[hep-th](#)]].
- [196] S. Pasterski, “A Chapter on Celestial Holography,” [[arXiv:2310.04932](#) [[hep-th](#)]].
- [197] A. Bagchi, P. Dhivakar and S. Dutta, “Holography in Flat Spacetimes: the case for Carroll,” [[arXiv:2311.11246](#) [[hep-th](#)]].
- [198] L. Donnay, A. Fiorucci, Y. Herfray and R. Ruzziconi, “Bridging Carrollian and celestial holography,” *Phys. Rev. D* **107**, no.12, 126027 (2023) doi:10.1103/PhysRevD.107.126027 [[arXiv:2212.12553](#) [[hep-th](#)]].
- [199] L. Donnay, A. Fiorucci, Y. Herfray and R. Ruzziconi, “Carrollian Perspective on Celestial Holography,” *Phys. Rev. Lett.* **129**, no.7, 071602 (2022) doi:10.1103/PhysRevLett.129.071602 [[arXiv:2202.04702](#) [[hep-th](#)]].
- 
- [200] D. A. Galante, “Modave lectures on de Sitter space & holography,” *PoS Modave2022*, 003 (2023) doi:10.22323/1.435.0003 [[arXiv:2306.10141](#) [[hep-th](#)]].
- [201] M. Spradlin, A. Strominger and A. Volovich, “Les Houches lectures on de Sitter space,” [[arXiv:hep-th/0110007](#) [[hep-th](#)]].

- [202] Y. Jiang, “A pedagogical review on solvable irrelevant deformations of 2D quantum field theory,” *Commun. Theor. Phys.* **73**, no.5, 057201 (2021) doi:10.1088/1572-9494/abe4c9 [[arXiv:1904.13376 \[hep-th\]](#)].
- 
- [203] I. Bah, D. S. Freed, G. W. Moore, N. Nekrasov, S. S. Razamat and S. Schafer-Nameki, “A Panorama Of Physical Mathematics c. 2022,” [[arXiv:2211.04467 \[hep-th\]](#)].
- [204] N. Garner and N. M. Paquette, “Mathematics of String Dualities,” *PoS TASI2021*, 007 (2023) doi:10.22323/1.403.0007 [[arXiv:2204.01914 \[hep-th\]](#)].
- [205] K. Hori, S. Katz, A. Klemm, R. Pandharipande, R. Thomas, C. Vafa, R. Vakil and E. Zaslow, “Mirror symmetry,” AMS, 2003, <https://www.claymath.org/library/monographs/cmim01.pdf>
- [206] P. S. Aspinwall, T. Bridgeland, A. Craw, M. R. Douglas, A. Kapustin, G. W. Moore, M. Gross, G. Segal, B. Szendrői and P. M. H. Wilson, “Dirichlet branes and mirror symmetry,” AMS, 2009, <https://www.claymath.org/library/monographs/cmim04.pdf>
- [207] Denis Auroux, <https://ocw.mit.edu/courses/18-969-topics-in-geometry-mirror-symmetry-spring-2009/pages/lecture-notes/>,
- [208] M. Alim, “Lectures on Mirror Symmetry and Topological String Theory,” [[arXiv:1207.0496 \[hep-th\]](#)].
- [209] K. Hori, “Trieste lectures on mirror symmetry,” *ICTP Lect. Notes Ser.* **13**, 109-202 (2003) <https://inspirehep.net/files/045fe862f3e8ab7b15300626a281ffaf>
- [210] A. Kapustin and D. Orlov, “Lectures on mirror symmetry, derived categories, and D-branes,” *Russ. Math. Surveys* **59**, 907 (2004) doi:10.1070/RM2004v059n05ABEH000772 [[arXiv:math/0308173 \[math.AG\]](#)].
- [211] S. Hosono, A. Klemm and S. Theisen, “Lectures on mirror symmetry,” *Lect. Notes Phys.* **436**, 235-280 (1994) doi:10.1007/3-540-58453-6\_13 [[arXiv:hep-th/9403096 \[hep-th\]](#)].
- [212] M. R. Ballard, “Meet homological mirror symmetry,” *Fields Inst. Commun.* **54**, 191-224 (2008) [[arXiv:0801.2014 \[math.AG\]](#)].
- [213] C. Quigley, “Mirror Symmetry in Physics: The Basics,” *Fields Inst. Monogr.* **34**, 211-278 (2015) doi:10.1007/978-1-4939-2830-9\_7 [[arXiv:1412.8180 \[hep-th\]](#)].
- [214] B. Haghighat, “Mirror Symmetry and Modularity,” [[arXiv:1712.00601 \[hep-th\]](#)].
- [215] A. Imparato, “Towards Homological Mirror Symmetry,” [[arXiv:2108.03931 \[math.SG\]](#)].
- [216] A. Imparato, “About Homological Mirror Symmetry,” [[arXiv:2306.13589 \[math.AG\]](#)].
- [217] B. Webster and P. Yoo, “3-dimensional mirror symmetry,” [[arXiv:2308.06191 \[math-ph\]](#)].
- 
- [218] E. D’Hoker and J. Kaidi, “Lectures on modular forms and strings,” [[arXiv:2208.07242 \[hep-th\]](#)].
- [219] V. Anagiannis and M. C. N. Cheng, “TASI Lectures on Moonshine,” *PoS TASI2017*, 010 (2018) doi:10.22323/1.305.0010 [[arXiv:1807.00723 \[hep-th\]](#)].
- [220] S. M. Harrison, J. A. Harvey and N. M. Paquette, “Snowmass White Paper: Moonshine,” [[arXiv:2201.13321 \[hep-th\]](#)].

- [221] J. F. R. Duncan, J. A. Harvey and B. C. Rayhaun, “An Overview of Penumbral Moonshine,” [[arXiv:2109.09756](#) [[math.RT](#)]].
- [222] V. Tatitscheff, “Monstrous Moonshine: A Short Introduction,” *Reson.* **27**, no.12, 2107-2126 (2022) doi:10.1007/s12045-022-1508-x [[arXiv:1902.03118](#) [[math.NT](#)]].
- [223] S. Gukov and I. Saberi, “Lectures on Knot Homology and Quantum Curves,” doi:10.1090/conm/613/12235 [[arXiv:1211.6075](#) [[hep-th](#)]].
- [224] S. Nawata and A. Oblomkov, “Lectures on knot homology,” *Contemp. Math.* **680**, 137 (2016) doi:10.1090/conm/680/13702 [[arXiv:1510.01795](#) [[math-ph](#)]].
- [225] E. Witten, “Geometric Langlands From Six Dimensions,” [[arXiv:0905.2720](#) [[hep-th](#)]].
- [226] E. Witten, “Mirror Symmetry, Hitchin’s Equations, And Langlands Duality,” doi:10.1093/acprof:oso/9780199534920.003.0007 [[arXiv:0802.0999](#) [[math.RT](#)]].
- [227] E. Witten, “Geometric Langlands And The Equations Of Nahm And Bogomolny,” [[arXiv:0905.4795](#) [[hep-th](#)]].
- [228] K. G. Schlesinger, “A Physics perspective on geometric Langlands duality,” [[arXiv:0911.4586](#) [[hep-th](#)]].
- [229] J. Evslin, “What does(n’t) K-theory classify?,” [[arXiv:hep-th/0610328](#) [[hep-th](#)]].
- [230] R. J. Szabo, “D-branes and bivariant K-theory,” [[arXiv:0809.3029](#) [[hep-th](#)]].
- [231] P. G. O. Freund, “p-adic strings and their applications,” *AIP Conf. Proc.* **826**, no.1, 65-73 (2006) doi:10.1063/1.2193111 [[arXiv:hep-th/0510192](#) [[hep-th](#)]].
- [232] B. Dragovich, A. Y. Khrennikov, S. V. Kozyrev and I. V. Volovich, “On p-Adic Mathematical Physics,” *Anal. Appl.* **1**, 1-17 (2009) [[arXiv:0904.4205](#) [[math-ph](#)]].
- [233] S. S. Gubser, C. Jepsen and B. Trundy, “Spin in  $p$ -adic AdS/CFT,” *J. Phys. A* **52**, no.14, 144004 (2019) doi:10.1088/1751-8121/ab0757 [[arXiv:1811.02538](#) [[hep-th](#)]].
- [234] B. Dragovich, A. Y. Khrennikov, S. V. Kozyrev, I. V. Volovich and E. I. Zelenov, “ $p$ -Adic Mathematical Physics: The First 30 Years,” *Anal. Appl.* **9**, 87-121 (2017) doi:10.1134/S2070046617020017 [[arXiv:1705.04758](#) [[math-ph](#)]].
- [235] L. Borsten, M. J. Farahani, B. Jurco, H. Kim, J. Narozny, D. Rist, C. Saemann and M. Wolf, “Higher Gauge Theory,” [[arXiv:2401.05275](#) [[hep-th](#)]].
- [236] B. Jurčo, C. Saemann, U. Schreiber and M. Wolf, “Higher Structures in M-Theory,” *Fortsch. Phys.* **67**, no.8-9, 1910001 (2019) doi:10.1002/prop.201910001 [[arXiv:1903.02807](#) [[hep-th](#)]].
- [237] D. Fiorenza, H. Sati and U. Schreiber, “The Rational Higher Structure of M-theory,” *Fortsch. Phys.* **67**, no.8-9, 1910017 (2019) doi:10.1002/prop.201910017 [[arXiv:1903.02834](#) [[hep-th](#)]].
- [238] T. Yoneya, “Lectures on Higher-Gauge Symmetries from Nambu Brackets and Covariantized M(atric) Theory,” [[arXiv:1612.08513](#) [[hep-th](#)]].
- [239] C. Saemann, “Lectures on Higher Structures in M-Theory,” doi:10.1142/9789813144613.0004 [[arXiv:1609.09815](#) [[hep-th](#)]].
- [240] Yuri Ximenes Martins, Rodney Josué Biezuner, “Higher Category Theory and Hilbert’s Sixth Problem,” 2020 [[hal:02909681](#)]
- [241] J. C. Baez and J. Huerta, “An Invitation to Higher Gauge Theory,” *Gen. Rel. Grav.* **43**, 2335-2392 (2011) doi:10.1007/s10714-010-1070-9 [[arXiv:1003.4485](#) [[hep-th](#)]].



- [242] H. Sati and U. Schreiber, “Mathematical foundations of quantum field theory and perturbative string theory,” Am. Math. Sci., 2011, ISBN 978-0-8218-5195-1
- 
- [243] M. Khalkhali, “Lectures on noncommutative geometry,” [[arXiv:math/0702140](#) [[math.QA](#)]].
- [244] V. Ginzburg, “Lectures on noncommutative geometry,” [[arXiv:math/0506603](#) [[math.AG](#)]].
- [245] F. D’Andrea, “Topics in Noncommutative Geometry,” [[arXiv:1510.07271](#) [[math.QA](#)]].
- [246] Snigdhasyan Mahanta, “On some approaches towards non-commutative algebraic geometry,” [[arXiv:math/0501166](#) [[math.QA](#)]].
- [247] P. Vitale, M. Adamo, R. Dekhil and D. Fernández-Silvestre, “Introduction to noncommutative field and gauge theory,” [[arXiv:2309.17369](#) [[hep-th](#)]].
- [248] M. R. Douglas and N. A. Nekrasov, “Noncommutative field theory,” Rev. Mod. Phys. **73**, 977-1029 (2001) doi:10.1103/RevModPhys.73.977 [[arXiv:hep-th/0106048](#) [[hep-th](#)]].
- [249] R. J. Szabo, “Quantum field theory on noncommutative spaces,” Phys. Rept. **378**, 207-299 (2003) doi:10.1016/S0370-1573(03)00059-0 [[arXiv:hep-th/0109162](#) [[hep-th](#)]].
- [250] V. P. Nair, “Noncommutative mechanics, Landau levels, twistors and Yang-Mills amplitudes,” Lect. Notes Phys. **698**, 97-138 (2006) doi:10.1007/3-540-33314-2\_3 [[arXiv:hep-th/0506120](#) [[hep-th](#)]].
- [251] P. Aschieri and L. Castellani, “Noncommutative gauge and gravity theories and geometric Seiberg–Witten map,” Eur. Phys. J. ST **232**, no.23-24, 3733-3746 (2023) doi:10.1140/epjs/s11734-023-00831-7 [[arXiv:2209.03774](#) [[hep-th](#)]].
- [252] R. J. Szabo and M. Tirelli, “Noncommutative instantons in diverse dimensions,” Eur. Phys. J. ST **232**, no.23-24, 3661-3680 (2023) doi:10.1140/epjs/s11734-023-00840-6 [[arXiv:2207.12862](#) [[hep-th](#)]].
- [253] A. P. Balachandran, S. Kurcuoglu and S. Vaidya, “Lectures on fuzzy and fuzzy SUSY physics,” [[arXiv:hep-th/0511114](#) [[hep-th](#)]].
- [254] B. Ydri, “Lectures on Matrix Field Theory,” Lect. Notes Phys. **929**, pp.1-352 (2017) Springer, 2017, ISBN 978-3-319-46002-4, 978-3-319-46003-1 doi:10.1007/978-3-319-46003-1 [[arXiv:1603.00924](#) [[hep-th](#)]].
- [255] I. Y. Arefeva, D. M. Belov, A. A. Giryavets, A. S. Koshelev and P. B. Medvedev, “Noncommutative field theories and (super)string field theories,” doi:10.1142/9789812777317\_0001 [[arXiv:hep-th/0111208](#) [[hep-th](#)]].
- [256] H. Steinacker, “Emergent Geometry and Gravity from Matrix Models: an Introduction,” Class. Quant. Grav. **27**, 133001 (2010) doi:10.1088/0264-9381/27/13/133001 [[arXiv:1003.4134](#) [[hep-th](#)]].
- [257] H. Steinacker, “Non-commutative geometry and matrix models,” PoS **QGQGS2011**, 004 (2011) doi:10.22323/1.140.0004 [[arXiv:1109.5521](#) [[hep-th](#)]].
- [258] F. Lizzi, “Noncommutative Geometry and Particle Physics,” PoS **CORFU2017**, 133 (2018) doi:10.22323/1.318.0133 [[arXiv:1805.00411](#) [[hep-th](#)]].
- [259] W. D. van Suijlekom, “Noncommutative geometry and particle physics,” Springer, 2015, ISBN 978-94-017-9161-8, 978-94-017-9162-5 doi:10.1007/978-94-017-9162-5
- [260] L. Bubuianu, D. Singleton, S. I. Vacaru and E. V. Veliev, “Nonassociative Geometric and Quantum Information Flows and R-Flux Deformations of Wormhole Solutions in String

- Gravity,” *Fortsch. Phys.* **72**, no.3, 2300212 (2024) doi:10.1002/prop.202300212 [[arXiv:2402.10993 \[hep-th\]](#)].
- [261] R. Blumenhagen and E. Plauschinn, “Nonassociative Gravity in String Theory?,” *J. Phys. A* **44**, 015401 (2011) doi:10.1088/1751-8113/44/1/015401 [[arXiv:1010.1263 \[hep-th\]](#)].
- [262] R. Blumenhagen and M. Fuchs, “Towards a Theory of Nonassociative Gravity,” *JHEP* **07**, 019 (2016) doi:10.1007/JHEP07(2016)019 [[arXiv:1604.03253 \[hep-th\]](#)].
- [263] D. Viennot, “Metrics and geodesics on fuzzy spaces,” [[arXiv:2305.15095 \[math-ph\]](#)].
- [264] G. Manolakos, P. Manousselis, D. Roumelioti, S. Stefas and G. Zoupanos, “Matrix-Formulated Noncommutative Gauge Theories of Gravity,” *PoS CORFU2021*, 285 (2022) doi:10.22323/1.406.0285 doi:10.22323/1.406.0285
- [265] G. Manolakos, P. Manousselis, D. Roumelioti, S. Stefas and G. Zoupanos, “Intertwining noncommutativity with gravity and particle physics,” *Eur. Phys. J. ST* **232**, no.23-24, 3607-3624 (2023) doi:10.1140/epjs/s11734-023-00830-8 [[arXiv:2305.11785 \[hep-th\]](#)].
- [266] A. H. Chamseddine, A. Connes and W. D. van Suijlekom, “Noncommutativity and physics: a non-technical review,” *Eur. Phys. J. ST* **232**, no.23-24, 3581-3588 (2023) doi:10.1140/epjs/s11734-023-00842-4 [[arXiv:2207.10901 \[hep-th\]](#)].
- [267] M. R. Douglas, “Two lectures on D-geometry and noncommutative geometry,” [[arXiv:hep-th/9901146 \[hep-th\]](#)].
- 
- [268] A. Dasgupta, H. Nicolai and J. Plefka, “An introduction to the quantum supermembrane,” *Grav. Cosmol.* **8**, 1 (2002) [[arXiv:hep-th/0201182 \[hep-th\]](#)].
- [269] M. J. Duff, “Supermembranes,” [[arXiv:hep-th/9611203 \[hep-th\]](#)].
- [270] H. Nicolai and R. Helling, “Supermembranes and M(atrix) theory,” [[arXiv:hep-th/9809103 \[hep-th\]](#)].
- [271] J. Hoppe, “Recent progress on Membrane Theory,” *PoS CORFU2021*, 258 (2022) doi:10.22323/1.406.0258 [inspirehep.net/files/c6839f351370b7328bd22bd19c381a20](#)
- [272] M. Cederwall, “Thoughts on membranes, matrices and non-commutativity,” [[arXiv:hep-th/0410110 \[hep-th\]](#)].
- [273] P. S. Howe and E. Sezgin, “The Supermembrane revisited,” *Class. Quant. Grav.* **22**, 2167-2200 (2005) doi:10.1088/0264-9381/22/11/017 [[arXiv:hep-th/0412245 \[hep-th\]](#)].
- [274] M. P. Garcia del Moral, “Dualities as symmetries of the Supermembrane Theory,” [[arXiv:1211.6265 \[hep-th\]](#)].
- [275] M. J. Duff, J. X. Lu, R. Percacci, C. N. Pope, H. Samtleben and E. Sezgin, “Membrane Duality Revisited,” *Nucl. Phys. B* **901**, 1-21 (2015) doi:10.1016/j.nuclphysb.2015.10.003 [[arXiv:1509.02915 \[hep-th\]](#)].
- [276] P. K. Townsend, “The eleven-dimensional supermembrane revisited,” *Phys. Lett. B* **350**, 184-187 (1995) doi:10.1016/0370-2693(95)00397-4 [[arXiv:hep-th/9501068 \[hep-th\]](#)].
- [277] G. Linardopoulos, “Classical Strings and Membranes in the AdS/CFT Correspondence,” [users.uoa.gr/~glinardo/Thesis.pdf](#)
- [278] Fiona K. Seibold and Arkady A. Tseytlin, “Scattering on the supermembrane,” [[arXiv:2404.09658 \[hep-th\]](#)].
-



- [279] W. Taylor, “M(atrrix) Theory: Matrix Quantum Mechanics as a Fundamental Theory,” *Rev. Mod. Phys.* **73**, 419-462 (2001) doi:10.1103/RevModPhys.73.419 [[arXiv:hep-th/0101126](#) [[hep-th](#)]].
- [280] W. Taylor, “The M(atrrix) model of M theory,” *NATO Sci. Ser. C* **556**, 91-178 (2000) doi:10.1007/978-94-011-4303-5\_3 [[arXiv:hep-th/0002016](#) [[hep-th](#)]].
- [281] B. Ydri, “Review of M(atrrix)-Theory, Type IIB Matrix Model and Matrix String Theory,” [[arXiv:1708.00734](#) [[hep-th](#)]].
- [282] A. Konechny and A. S. Schwarz, “Introduction to M(atrrix) theory and noncommutative geometry,” *Phys. Rept.* **360**, 353-465 (2002) doi:10.1016/S0370-1573(01)00096-5 [[arXiv:hep-th/0012145](#) [[hep-th](#)]].
- [283] A. Konechny and A. S. Schwarz, “Introduction to M(atrrix) theory and noncommutative geometry. Part 2.,” [[arXiv:hep-th/0107251](#) [[hep-th](#)]].
- [284] D. Bigatti and L. Susskind, “Review of matrix theory,” *NATO Sci. Ser. C* **520**, 277-318 (1999) [[arXiv:hep-th/9712072](#) [[hep-th](#)]].
- [285] T. Banks, “TASI lectures on matrix theory,” [[arXiv:hep-th/9911068](#) [[hep-th](#)]].
- 
- [286] N. B. Copland, “Introductory Lectures on Multiple Membranes,” [[arXiv:1012.0459](#) [[hep-th](#)]].
- [287] J. Bagger, N. Lambert, S. Mukhi and C. Papageorgakis, “Multiple Membranes in M-theory,” *Phys. Rept.* **527**, 1-100 (2013) doi:10.1016/j.physrep.2013.01.006 [[arXiv:1203.3546](#) [[hep-th](#)]].
- [288] I. R. Klebanov and G. Torri, “M2-branes and AdS/CFT,” *Int. J. Mod. Phys. A* **25**, 332-350 (2010) doi:10.1142/S0217751X10048652 [[arXiv:0909.1580](#) [[hep-th](#)]].
- [289] N. Lambert, “M-Branes: Lessons from M2’s and Hopes for M5’s,” *Fortsch. Phys.* **67**, no.8-9, 1910011 (2019) doi:10.1002/prop.201910011 [[arXiv:1903.02825](#) [[hep-th](#)]].
- [290] K. Hosomichi, “M2-branes and AdS/CFT: A Review,” *PTEP* **2020**, no.11, 11B102 (2020) doi:10.1093/ptep/ptaa060 [[arXiv:2003.13914](#) [[hep-th](#)]].
- [291] R. Dijkgraaf, S. Gukov, A. Neitzke and C. Vafa, “Topological M-theory as unification of form theories of gravity,” *Adv. Theor. Math. Phys.* **9**, no.4, 603-665 (2005) doi:10.4310/ATMP.2005.v9.n4.a5 [[arXiv:hep-th/0411073](#) [[hep-th](#)]].
- [292] P. C. West, “E(11) and M theory,” *Class. Quant. Grav.* **18**, 4443-4460 (2001) doi:10.1088/0264-9381/18/21/305 [[arXiv:hep-th/0104081](#) [[hep-th](#)]].
- [293] G. T. Horowitz and L. Susskind, “Bosonic M theory,” *J. Math. Phys.* **42**, 3152-3160 (2001) doi:10.1063/1.1376160 [[arXiv:hep-th/0012037](#) [[hep-th](#)]].
- [294] K. S. Kim, A. Mitra, D. Mukherjee and S. Ryu, “Monotonicity of renormalization group flow, Perelman’s entropy functional, and emergent dual holography in the worldsheet nonlinear  $\sigma$  model,” [[arXiv:2404.09122](#) [[hep-th](#)]].
- 
- [295] C. Maccaferri, “String Field Theory,” [[arXiv:2308.00875](#) [[hep-th](#)]].
- [296] C. de Lacroix, H. Erbin, S. P. Kashyap, A. Sen and M. Verma, “Closed Superstring Field Theory and its Applications,” *Int. J. Mod. Phys. A* **32**, no.28n29, 1730021 (2017) doi:10.1142/S0217751X17300216 [[arXiv:1703.06410](#) [[hep-th](#)]].
- [297] T. Erler, “Four Lectures on Closed String Field Theory,” *Phys. Rept.* **851**, 1-36 (2020) doi:10.1016/j.physrep.2020.01.003 [[arXiv:1905.06785](#) [[hep-th](#)]].

- [298] T. Erler, “Four lectures on analytic solutions in open string field theory,” *Phys. Rept.* **980**, 1-95 (2022) doi:10.1016/j.physrep.2022.06.004 [[arXiv:1912.00521 \[hep-th\]](#)].
- [299] E. Fuchs and M. Kroyter, “Analytical Solutions of Open String Field Theory,” *Phys. Rept.* **502**, 89-149 (2011) doi:10.1016/j.physrep.2011.01.003 [[arXiv:0807.4722 \[hep-th\]](#)].
- [300] Y. Okawa, “Analytic methods in open string field theory,” *Prog. Theor. Phys.* **128**, 1001-1060 (2012) doi:10.1143/PTP.128.1001
- [301] W. Taylor, “String field theory,” [[arXiv:hep-th/0605202 \[hep-th\]](#)].
- [302] L. Rastelli, “String field theory,” [[arXiv:hep-th/0509129 \[hep-th\]](#)].
- [303] A. Sen, “String Field Theory as World-sheet UV Regulator,” *JHEP* **10**, 119 (2019) doi:10.1007/JHEP10(2019)119 [[arXiv:1902.00263 \[hep-th\]](#)].
- [304] W. Siegel, “Introduction to string field theory,” *Adv. Ser. Math. Phys.* **8**, 1-244 (1988) [[arXiv:hep-th/0107094 \[hep-th\]](#)].
- [305] A. Sen, “Tachyon dynamics in open string theory,” *Int. J. Mod. Phys. A* **20**, 5513-5656 (2005) doi:10.1142/S0217751X0502519X [[arXiv:hep-th/0410103 \[hep-th\]](#)].
- [306] M. Headrick, S. Minwalla and T. Takayanagi, “Closed string tachyon condensation: An Overview,” *Class. Quant. Grav.* **21**, S1539-S1565 (2004) doi:10.1088/0264-9381/21/10/027 [[arXiv:hep-th/0405064 \[hep-th\]](#)].
- [307] W. Taylor and B. Zwiebach, “D-branes, tachyons, and string field theory,” doi:10.1142/9789812702821\_0012 [[arXiv:hep-th/0311017 \[hep-th\]](#)].
- [308] W. Taylor, “Lectures on D-branes, tachyon condensation, and string field theory,” doi:10.1007/0-387-24992-3\_4 [[arXiv:hep-th/0301094 \[hep-th\]](#)].
- [309] J. Gomis, “Lectures on tachyon condensation: Towards time-dependent backgrounds and holography,” *Class. Quant. Grav.* **22**, S107-S124 (2005) doi:10.1088/0264-9381/22/8/004
- 
- [310] A. Dabholkar and S. Nampuri, “Quantum black holes,” *Lect. Notes Phys.* **851**, 165-232 (2012) doi:10.1007/978-3-642-25947-0\_5 [[arXiv:1208.4814 \[hep-th\]](#)].
- [311] N. P. Warner, “Lectures on Microstate Geometries,” [[arXiv:1912.13108 \[hep-th\]](#)].
- [312] A. Zaffaroni, “AdS black holes, holography and localization,” *Living Rev. Rel.* **23**, no.1, 2 (2020) doi:10.1007/s41114-020-00027-8 [[arXiv:1902.07176 \[hep-th\]](#)].
- [313] L. Martucci, N. Risso, A. Valenti and L. Vecchi, “Wormholes in the axiverse, and the species scale,” [[arXiv:2404.14489 \[hep-th\]](#)].
- [314] A. Hebecker, T. Mikhail and P. Soler, “Euclidean wormholes, baby universes, and their impact on particle physics and cosmology,” *Front. Astron. Space Sci.* **5**, 35 (2018) doi:10.3389/fspas.2018.00035 [[arXiv:1807.00824 \[hep-th\]](#)].
- [315] D. Grabovsky, “Chern–Simons Theory in a Knotshell,” <https://web.physics.ucsb.edu/~davidgrabovsky/files-notes/CS%20and%20Knots.pdf>
- [316] G. V. Dunne, “Aspects of Chern-Simons theory,” [[arXiv:hep-th/9902115 \[hep-th\]](#)].
- [317] J. M. F. Labastida, “Chern-Simons gauge theory: Ten years after,” *AIP Conf. Proc.* **484**, no.1, 1-40 (1999) doi:10.1063/1.59663 [[arXiv:hep-th/9905057 \[hep-th\]](#)].
- [318] R. K. Kaul, T. R. Govindarajan and P. Ramadevi, “Schwarz type topological quantum field theories,” [[arXiv:hep-th/0504100 \[hep-th\]](#)].

- [319] S. Carlip, “Quantum Gravity in 2+1 Dimensions,” [[arXiv:2312.12596 \[gr-qc\]](#)].
- [320] S. Carlip, “Conformal field theory, (2+1)-dimensional gravity, and the BTZ black hole,” *Class. Quant. Grav.* **22**, R85-R124 (2005) doi:10.1088/0264-9381/22/12/R01 [[arXiv:gr-qc/0503022 \[gr-qc\]](#)].
- [321] S. Carlip, “Quantum gravity in 2+1 dimensions,” Cambridge University Press, 2003, ISBN 978-0-521-54588-4, 978-0-511-82229-2 doi:10.1017/CBO9780511564192
- [322] S. Carlip, “Quantum gravity in 2+1 dimensions: The Case of a closed universe,” *Living Rev. Rel.* **8**, 1 (2005) doi:10.12942/lrr-2005-1 [[arXiv:gr-qc/0409039 \[gr-qc\]](#)].
- [323] S. Carlip, “Lectures on (2+1) dimensional gravity,” *J. Korean Phys. Soc.* **28**, S447-S467 (1995) [[arXiv:gr-qc/9503024 \[gr-qc\]](#)].
- 
- [324] M. Vonk, “A Mini-course on topological strings,” [[arXiv:hep-th/0504147 \[hep-th\]](#)].
- [325] A. Neitzke and C. Vafa, “Topological strings and their physical applications,” [[arXiv:hep-th/0410178 \[hep-th\]](#)].
- [326] A. Klemm, “Topological string theory on Calabi-Yau threefolds,” *PoS RTN2005*, 002 (2005) doi:10.22323/1.019.0002
- [327] L. Ferro and T. Lukowski, “Amplituhedra, and beyond,” *J. Phys. A* **54**, no.3, 033001 (2021) doi:10.1088/1751-8121/abd21d [[arXiv:2007.04342 \[hep-th\]](#)].
- [328] E. Herrmann and J. Trnka, “The SAGEX review on scattering amplitudes Chapter 7: Positive geometry of scattering amplitudes,” *J. Phys. A* **55**, no.44, 443008 (2022) doi:10.1088/1751-8121/ac8709 [[arXiv:2203.13018 \[hep-th\]](#)].
- [329] Z. Bern and J. Trnka, “Snowmass TF04 Report: Scattering Amplitudes and their Applications,” [[arXiv:2210.03146 \[hep-th\]](#)].
- [330] G. Travaglini, A. Brandhuber, P. Dorey, T. McLoughlin, S. Abreu, Z. Bern, N. E. J. Bjerrum-Bohr, J. Blümlein, R. Britto and J. J. M. Carrasco, *et al.* “The SAGEX review on scattering amplitudes,” *J. Phys. A* **55**, no.44, 443001 (2022) doi:10.1088/1751-8121/ac8380 [[arXiv:2203.13011 \[hep-th\]](#)].
- [331] J. J. M. Carrasco, “Gauge and Gravity Amplitude Relations,” doi:10.1142/9789814678766\_0011 [[arXiv:1506.00974 \[hep-th\]](#)].
- [332] J. J. Carrasco, “TASI 2022 lectures on scattering amplitudes – an addendum,” *PoS TASI2022*, 002 (2024) doi:10.22323/1.439.0002
- [333] T. Adamo, J. J. M. Carrasco, M. Carrillo-González, M. Chiodaroli, H. Elvang, H. Johansson, D. O’Connell, R. Roiban and O. Schlotterer, “Snowmass White Paper: the Double Copy and its Applications,” [[arXiv:2204.06547 \[hep-th\]](#)].
- 
- [334] V. Pestun, M. Zabzine, F. Benini, T. Dimofte, T. T. Dumitrescu, K. Hosomichi, S. Kim, K. Lee, B. Le Floch and M. Marino, *et al.* “Localization techniques in quantum field theories,” *J. Phys. A* **50**, no.44, 440301 (2017) doi:10.1088/1751-8121/aa63c1 [[arXiv:1608.02952 \[hep-th\]](#)].
- [335] D. R. Morrison, “Gromov–Witten invariants and localization,” *J. Phys. A* **50**, no.44, 443004 (2017) doi:10.1088/1751-8121/aa6f65 [[arXiv:1608.02956 \[hep-th\]](#)].

- [336] K. Zarembo, “Localization and AdS/CFT Correspondence,” *J. Phys. A* **50**, no.44, 443011 (2017) doi:10.1088/1751-8121/aa585b [[arXiv:1608.02963 \[hep-th\]](#)].
- 
- [337] C. Cordova, T. T. Dumitrescu, K. Intriligator and S. H. Shao, “Snowmass White Paper: Generalized Symmetries in Quantum Field Theory and Beyond,” [[arXiv:2205.09545 \[hep-th\]](#)].
- [338] T. D. Brennan and S. Hong, “Introduction to Generalized Global Symmetries in QFT and Particle Physics,” [[arXiv:2306.00912 \[hep-ph\]](#)].
- [339] L. Bhardwaj, L. E. Bottini, L. Fraser-Taliente, L. Gladden, D. S. W. Gould, A. Platschorre and H. Tillim, “Lectures on generalized symmetries,” *Phys. Rept.* **1051**, 1-87 (2024) doi:10.1016/j.physrep.2023.11.002 [[arXiv:2307.07547 \[hep-th\]](#)].
- [340] S. H. Shao, “What’s Done Cannot Be Undone: TASI Lectures on Non-Invertible Symmetries,” [[arXiv:2308.00747 \[hep-th\]](#)].
- [341] S. Schafer-Nameki, “ICTP lectures on (non-)invertible generalized symmetries,” *Phys. Rept.* **1063**, 1-55 (2024) doi:10.1016/j.physrep.2024.01.007 [[arXiv:2305.18296 \[hep-th\]](#)].
- [342] P. R. S. Gomes, “An introduction to higher-form symmetries,” *SciPost Phys. Lect. Notes* **74**, 1 (2023) doi:10.21468/SciPostPhysLectNotes.74 [[arXiv:2303.01817 \[hep-th\]](#)].
- 
- [343] M. Cederwall, “Pure Spinors in Classical and Quantum Supergravity,” doi:10.1007/978-981-19-3079-9\_47-1 [[arXiv:2210.06141 \[hep-th\]](#)].
- [344] N. Berkovits and C. R. Mafra, “Pure Spinor Formulation of the Superstring and Its Applications,” doi:10.1007/978-981-19-3079-9\_63-1 [[arXiv:2210.10510 \[hep-th\]](#)].
- [345] N. Berkovits and H. Gomez, “An Introduction to Pure Spinor Superstring Theory,” doi:10.1007/978-3-319-65427-0\_6 [[arXiv:1711.09966 \[hep-th\]](#)].
- [346] O. Corradini, C. Schubert, J. P. Edwards and N. Ahmadinia, “Spinning Particles in Quantum Mechanics and Quantum Field Theory,” [[arXiv:1512.08694 \[hep-th\]](#)].
- [347] J. P. Edwards and C. Schubert, “Quantum mechanical path integrals in the first quantised approach to quantum field theory,” [[arXiv:1912.10004 \[hep-th\]](#)].
- [348] C. Schubert, “Perturbative quantum field theory in the string inspired formalism,” *Phys. Rept.* **355**, 73-234 (2001) doi:10.1016/S0370-1573(01)00013-8 [[arXiv:hep-th/0101036 \[hep-th\]](#)].
- [349] Vyacheslav Lysov, “Spinors and SUSY on a worldline,” [groups.oist.jp/system/files/WL\\_SUSY.pdf](#).
- [350] G. Oling and Z. Yan, “Aspects of Nonrelativistic Strings,” *Front. in Phys.* **10**, 832271 (2022) doi:10.3389/fphy.2022.832271 [[arXiv:2202.12698 \[hep-th\]](#)].
- [351] S. Baiguera, “Aspects of non-relativistic quantum field theories,” *Eur. Phys. J. C* **84**, no.3, 268 (2024) doi:10.1140/epjc/s10052-024-12630-y [[arXiv:2311.00027 \[hep-th\]](#)].
- [352] E. J. Martinec, “Matrix models and 2D string theory,” [[arXiv:hep-th/0410136 \[hep-th\]](#)].
- [353] P. H. Ginsparg and G. W. Moore, “Lectures on 2-D gravity and 2-D string theory,” [[arXiv:hep-th/9304011 \[hep-th\]](#)].
- [354] S. Chatterjee and E. Witten, “Liouville Theory: An Introduction to Rigorous Approaches,” [[arXiv:2404.02001 \[hep-th\]](#)].

- [355] Y. Nakayama, “Liouville field theory: A Decade after the revolution,” *Int. J. Mod. Phys. A* **19**, 2771-2930 (2004) doi:10.1142/S0217751X04019500 [arXiv:hep-th/0402009 [hep-th]].
- [356] J. Teschner, “Liouville theory revisited,” *Class. Quant. Grav.* **18**, R153-R222 (2001) doi:10.1088/0264-9381/18/23/201 [arXiv:hep-th/0104158 [hep-th]].
- [357] D. Grumiller and R. Meyer, “Ramifications of lineland,” *Turk. J. Phys.* **30**, 349-378 (2006) [arXiv:hep-th/0604049 [hep-th]].
- [358] D. Grumiller, W. Kummer and D. V. Vassilevich, “Dilaton gravity in two-dimensions,” *Phys. Rept.* **369**, 327-430 (2002) doi:10.1016/S0370-1573(02)00267-3 [arXiv:hep-th/0204253 [hep-th]].
- [359] L. Freidel, R. G. Leigh and D. Minic, “Modular Spacetime and Metastring Theory,” *J. Phys. Conf. Ser.* **804**, no.1, 012032 (2017) <https://doi.org/10.1088/1742-6596/804/1/012032>
- [360] I. Jeon, K. Lee and J. H. Park, “Stringy differential geometry, beyond Riemann,” *Phys. Rev. D* **84**, 044022 (2011) doi:10.1103/PhysRevD.84.044022 [arXiv:1105.6294 [hep-th]].
- 
- [361] T. Adamo, “Lectures on twistor theory,” *PoS Modave2017*, 003 (2018) doi:10.22323/1.323.0003 [arXiv:1712.02196 [hep-th]].
- [362] M. Atiyah, M. Dunajski and L. Mason, “Twistor theory at fifty: from contour integrals to twistor strings,” *Proc. Roy. Soc. Lond. A* **473**, no.2206, 20170530 (2017) doi:10.1098/rspa.2017.0530 [arXiv:1704.07464 [hep-th]].
- [363] T. Adamo, “Twistor actions for gauge theory and gravity,” [arXiv:1308.2820 [hep-th]].
- [364] T. Adamo, M. Bullimore, L. Mason and D. Skinner, “Scattering Amplitudes and Wilson Loops in Twistor Space,” *J. Phys. A* **44**, 454008 (2011) doi:10.1088/1751-8113/44/45/454008 [arXiv:1104.2890 [hep-th]].
- [365] M. Wolf, “A First Course on Twistors, Integrability and Gluon Scattering Amplitudes,” *J. Phys. A* **43**, 393001 (2010) doi:10.1088/1751-8113/43/39/393001 [arXiv:1001.3871 [hep-th]].
- [366] F. Cachazo and P. Svrcek, “Lectures on twistor strings and perturbative Yang-Mills theory,” *PoS RTN2005*, 004 (2005) doi:10.22323/1.019.0005 [arXiv:hep-th/0504194 [hep-th]].
- [367] R. Penrose, “[The Road to Reality: A Complete Guide to the Laws of the Universe](#),”
- [368] Ljudmila Kamenova, “Twistor spaces and compact manifolds admitting both Kähler and non-Kähler structures,” [arXiv:1711.07948 [math.DG]].
- [369] Y. Geyer and L. Mason, “The SAGEX review on scattering amplitudes Chapter 6: Ambitwistor Strings and Amplitudes from the Worldsheet,” *J. Phys. A* **55**, no.44, 443007 (2022) doi:10.1088/1751-8121/ac8190 [arXiv:2203.13017 [hep-th]].
- [370] M. Dunajski, “Twistor Theory and Differential Equations,” *J. Phys. A* **42**, 404004 (2009) doi:10.1088/1751-8113/42/40/404004 [arXiv:0902.0274 [hep-th]].
- [371] T. Adamo, D. Skinner and J. Williams, “Minitwistors and 3d Yang-Mills-Higgs theory,” *J. Math. Phys.* **59**, no.12, 122301 (2018) doi:10.1063/1.5030417 [arXiv:1712.09604 [hep-th]].
- [372] M. Carrillo González, W. T. Emond, N. Moynihan, J. Rumbutis and C. D. White, “Mini-twistors and the Cotton double copy,” *JHEP* **03**, 177 (2023) doi:10.1007/JHEP03(2023)177 [arXiv:2212.04783 [hep-th]].

- [373] D. W. Chiou, O. J. Ganor, Y. P. Hong, B. S. Kim and I. Mitra, “Massless and massive three dimensional super Yang-Mills theory and mini-twistor string theory,” *Phys. Rev. D* **71**, 125016 (2005) doi:10.1103/PhysRevD.71.125016 [[arXiv:hep-th/0502076](#) [[hep-th](#)]].
- [374] Nobuhiro Honda and Fuminori Nakata, “Minitwistor spaces, Severi varieties, and Einstein-Weyl structure,” [[arXiv:0901.2264](#) [[math.DG](#)]].
- [375] M. Dunajski, “Equivalence principle, de-Sitter space, and cosmological twistors,” *Int. J. Mod. Phys. D* **32**, no.14, 2341001 (2023) doi:10.1142/S0218271823410018 [[arXiv:2304.08574](#) [[gr-qc](#)]].
- [376] P. Woit, “Notes on the Twistor  $\mathbf{P}^1$ ,” [[arXiv:2202.02657](#) [[math-ph](#)]].
- [377] Peter Scholze, “ $p$ -adic geometry,” [[arXiv:1712.03708](#) [[math.AG](#)]].
- 
- [378] F. Cianfrani, O. M. Lecian and G. Montani, “Fundamentals and recent developments in non-perturbative canonical Quantum Gravity,” [[arXiv:0805.2503](#) [[gr-qc](#)]].
- [379] F. Cianfrani, O. M. Lecian, M. Lulli and G. Montani, “Canonical Quantum Gravity Fundamentals and Recent Developments,” <https://doi.org/10.1142/8957> — July 2014
- [380] A. Corichi and D. Núñez, “Introduction to the ADM formalism,” *Rev. Mex. Fis.* **37**, 720-747 (1991) [[arXiv:2210.10103](#) [[gr-qc](#)]].
- [381] A. Ashtekar and E. Bianchi, “A short review of loop quantum gravity,” *Rept. Prog. Phys.* **84**, no.4, 042001 (2021) doi:10.1088/1361-6633/abed91 [[arXiv:2104.04394](#) [[gr-qc](#)]].
- [382] N. Bodendorfer, “An elementary introduction to loop quantum gravity,” [[arXiv:1607.05129](#) [[gr-qc](#)]].
- [383] A. Ashtekar, M. Reuter and C. Rovelli, “From General Relativity to Quantum Gravity,” [[arXiv:1408.4336](#) [[gr-qc](#)]].
- [384] C. Rovelli and F. Vidotto, “Covariant Loop Quantum Gravity: An Elementary Introduction to Quantum Gravity and Spinfoam Theory,” Cambridge University Press, 2014, ISBN 978-1-107-06962-6, 978-1-316-14729-0 doi:10.1017/CBO9781107706910
- [385] C. Rovelli, “Zakopane lectures on loop gravity,” *PoS QGQGS2011*, 003 (2011) doi:10.22323/1.140.0003 [[arXiv:1102.3660](#) [[gr-qc](#)]].
- [386] C. Rovelli, “Quantum gravity,” *Univ. Pr.*, 2004, doi:10.1017/CBO9780511755804
- [387] T. Thiemann, “Modern canonical quantum general relativity,” [[arXiv:gr-qc/0110034](#) [[gr-qc](#)]].
- [388] H. Nicolai, K. Peeters and M. Zamaklar, “Loop quantum gravity: An Outside view,” *Class. Quant. Grav.* **22**, R193 (2005) doi:10.1088/0264-9381/22/19/R01 [[arXiv:hep-th/0501114](#) [[hep-th](#)]].
- [389] T. Thiemann, “Loop Quantum Gravity: An Inside View,” *Lect. Notes Phys.* **721**, 185-263 (2007) doi:10.1007/978-3-540-71117-9\_10 [[arXiv:hep-th/0608210](#) [[hep-th](#)]].
- [390] A. Ashtekar and P. Singh, “Loop Quantum Cosmology: A Status Report,” *Class. Quant. Grav.* **28**, 213001 (2011) doi:10.1088/0264-9381/28/21/213001 [[arXiv:1108.0893](#) [[gr-qc](#)]].
- 
- [391] A. Bonanno, A. Eichhorn, H. Gies, J. M. Pawłowski, R. Percacci, M. Reuter, F. Saueressig and G. P. Vacca, “Critical reflections on asymptotically safe gravity,” *Front. in Phys.* **8**, 269 (2020) doi:10.3389/fphy.2020.00269 [[arXiv:2004.06810](#) [[gr-qc](#)]].

- [392] R. Percacci, “Asymptotic Safety,” [[arXiv:0709.3851 \[hep-th\]](#)].
- [393] A. Platania, “Black Holes in Asymptotically Safe Gravity,” doi:10.1007/978-981-19-3079-9\_24-1 [[arXiv:2302.04272 \[gr-qc\]](#)].
- [394] S. Surya, “The causal set approach to quantum gravity,” *Living Rev. Rel.* **22**, no.1, 5 (2019) doi:10.1007/s41114-019-0023-1 [[arXiv:1903.11544 \[gr-qc\]](#)].
- [395] Y. K. Yazdi, “Everything you always wanted to know about how causal set theory can help with open questions in cosmology, but were afraid to ask,” *Mod. Phys. Lett. A* **39**, no.01, 2330003 (2024) doi:10.1142/S0217732323300033 [[arXiv:2311.14881 \[gr-qc\]](#)].
- [396] F. Finster, “Causal fermion systems: Classical gravity and beyond,” doi:10.1142/9789811269776\_0050 [[arXiv:2109.05906 \[gr-qc\]](#)].
- [397] F. Finster, “The Continuum Limit of Causal Fermion Systems,” Springer, 2016, doi:10.1007/978-3-319-42067-7 [[arXiv:1605.04742 \[math-ph\]](#)].
- [398] R. Loll, “Quantum Gravity from Causal Dynamical Triangulations: A Review,” *Class. Quant. Grav.* **37**, no.1, 013002 (2020) doi:10.1088/1361-6382/ab57c7 [[arXiv:1905.08669 \[hep-th\]](#)].
- [399] L. Freidel, “Group field theory: An Overview,” *Int. J. Theor. Phys.* **44**, 1769-1783 (2005) doi:10.1007/s10773-005-8894-1 [[arXiv:hep-th/0505016 \[hep-th\]](#)].
- [400] D. Oriti, “The Group field theory approach to quantum gravity,” [[arXiv:gr-qc/0607032 \[gr-qc\]](#)].
- [401] E. Alvarez and E. Velasco-Aja, “A Primer on Unimodular Gravity,” doi:10.1007/978-981-19-3079-9\_15-1 [[arXiv:2301.07641 \[gr-qc\]](#)].
- [402] M. Herrero-Valea, “The status of Hořava gravity,” *Eur. Phys. J. Plus* **138**, no.11, 968 (2023) doi:10.1140/epjp/s13360-023-04593-y [[arXiv:2307.13039 \[gr-qc\]](#)].



## Acknowledgments

I acknowledge that life is meaningless. I thank the fundamental laws of physics for being mathematically comprehensible and mysterious, but I will not thank the laws of physics for being amoral and absurdly pointless.

